3

OM

Sygal Patel

Ec E

PM 1(B)

ACE

Signals & Systems

0 () \bigcirc () () ٩ $\widehat{\mathbb{G}}$ 0 \bigcirc ()

	signals	and	Sustems	; ·	
9					
Anaiysi	S Apr	or ximat	ion	Tounsto	rmation
1 Introduction	M . O	Fourier	Series હ	() (.T.	
2 L.T.I. S	Azfemz				- F. T.
				4 7.7	
=> Books:				② D.	F.T.
1 apenhiv	im & Nac	wub.			
	13 & Vcm	Yeem -	2 <u>3</u> T		
3 2 & 5	e uzh gd	Romjan	M (Im	h).	
* Signal:					
0 => Signal	js cm	Indica	tion	about	which
Some	amount	ob '	nforma	tion i	2
Conveyed					
=> Random			ntorma		
i.e. Lhe			ch a	ie are	dont
	w s's si				
) () => The OPE	excetions :	In at	are pe	e storm	∞
•	iais are:				
© Enho	incing, (a) Filt	rsing.		
© Exter	acting		~		
3 540 8	ing				

Characterstics Ob a Signal:
=> 1) More than one independent harable
e.g.: (1) Speech -> 1D (Lime)
② Image -> 20 F I(x,y) pixel
3) T.y. picture -> 30
I (x, 4, 2).
=> @ Rundomness:
=> More the Rundomness more the
information. $I = log_2 \frac{1}{Pi} = -log_2 Pi$
: P; = 1/8 => I = 3 bits

(J

 $(\dot{})$

()

(i)

.: $P_i = \frac{1}{8} \Rightarrow I = 3 \text{ bits}$ more random. $\Rightarrow P_i = \frac{1}{32} \Rightarrow I = 5 \text{ bits}$.

=> In order to know the BW ob
the Channel we Should know the
BW of signal that's why the BW
is one of the Chara. Ob signal.

A Types ob signal: signal: 1 Continuous time occurs for Continumn A Signal which Value ob lime. is called Confirmons signal. the amplitude of the => At any instant Signal is known. => Continuous both in time and amp. is Continuon Signal. signal Type Time e.g. x(t)= e3t, u(t) Amp Conti-signer C Discrete signal (tox) D onuntizer C Digital D signou => Whenever there is sudden changes in the sixpored level (0%) amp is called Discontimuony signar. e.g. yct) signal. at 1=0,1,2 frese ase y(+) 1 Sudden Change in amp. so, at t=0,1,2, yct) the amp. is not. defined i.e. discontinuoy Pière-wise Biscontinuous

2) Biscrete signal: => A signal which is continuous in ampiitude but discrete en time Cinteger raines of time index). Is () Carred discrete signal. => Bw will be less than continuous signal. () ()=> Used in Concept of Multiple king which is very easy. => Sampiing: x (+) t=nt, n= 0, ±1, ±2, ±3,... Ts = Sampling sime. $\Rightarrow x(t) = e^{-3t}$. u(t). $x[nT_s] = e^{-3nT_s}$ u[nT_s] x(t)Let, Ts=1Sec $\propto (n) = e^{-3n}$ u[n]. cm3x <- [ITM] x x[n] for simplicity $x[nT_s - T_s] \rightarrow x[n-1]$ Ts is depend on samp. theorem. i.e. Is > 2 fm.

T₅ 27, 37, 47, ...

 $x[nT_s] \rightarrow x[n]$ for simplicity. So, we can't use $T_s=1$ sec

So, we can't use size see

Almost complitude ure some for au the Sample.

=> The Purpose of Sampling is multiplexing.

=> Every discrete signal is not the

Sampled Version of the Continuous signal
Some of the discrete signals are
Predetine.

Note:

Amp. Conversion from C->0 => Ougntizer

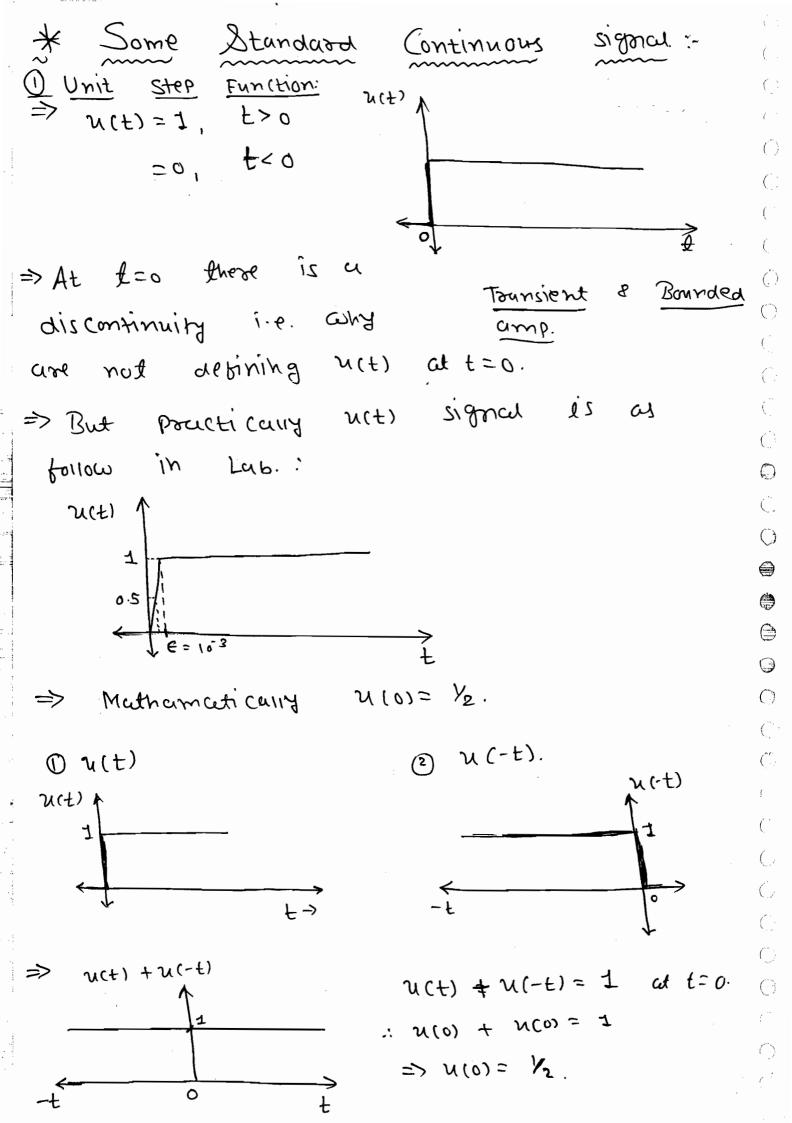
=> time Conversion from C->0 => Sampling.

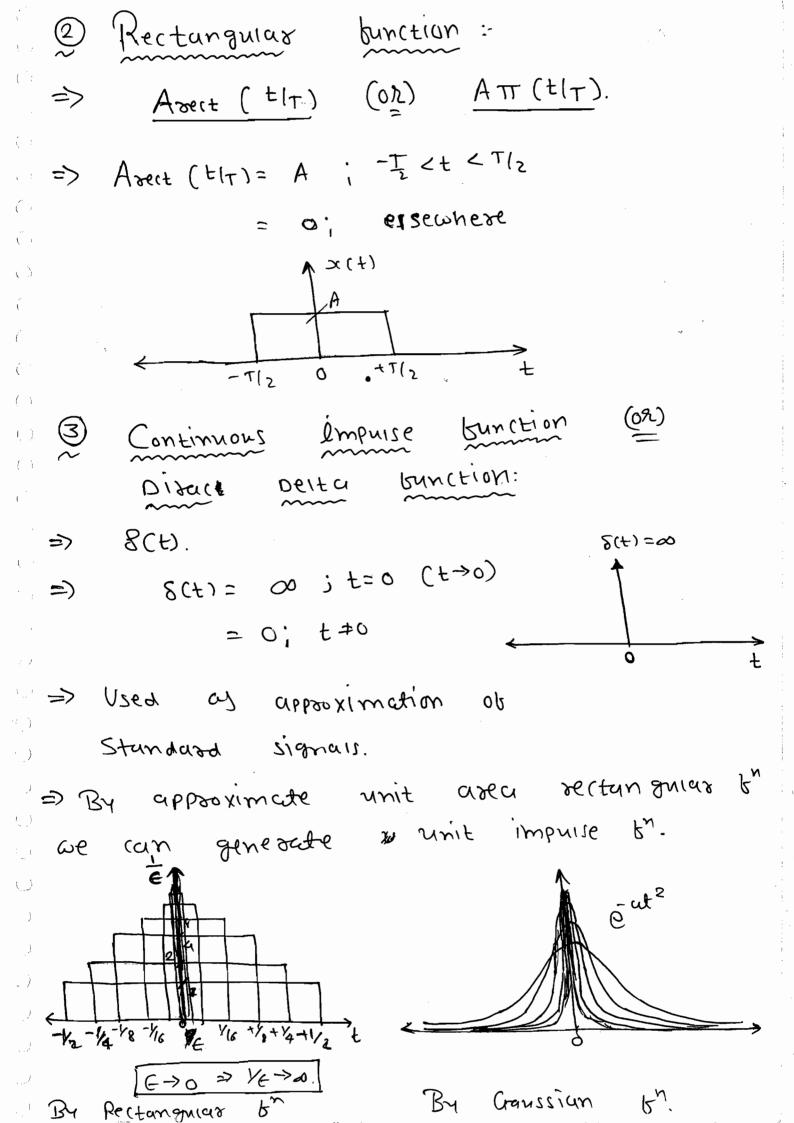
3 Digital Signal:

=> A signal which discrete in time and amplitude (quantized amp) is called Digital signal.

=> Ouantizer is used to Convert the Continuous comp. Signal into discrete comp. Signal into discrete comp. Signal.

Signal into discrete lime signal.





884X 23 Xis x(t) = 38(t). \Rightarrow 1.e. comp. = 3 but $camp = \infty$. but crosen under 8(t)=3. * Booberfiel OR Ect) P. (i) $\int_{0}^{+\infty} 8(t)^{2} = 1.$ Area Concept are used in (ii) 18(dt)= 1/41.8(t). Continuous 8 fn. (or) cont. d> Scaling factor. inpuise br. (iii) Product (Or) Sampling: 1 IMP → x(+). 8(+-+0) = x(+0). 8(+-+0) ib x(+)is Cont' cs t= to. to -> time shibt. 69. 0 Cost. S(+-TT). シャナリーサ = (0)TT = -1.t. 8(t) = to. 8(t) 2 as to=0 = 0.8(+) f.8(f) = 0 (iv) g(f) = g(-f)

0

()

 Θ

 \bigcirc

 \in

()

0

(_)

Shit ting: x(t). $8(t-t_0) dt = x(t_0); t_1 \leq t_0 \leq t_2$ = 0; eisewhere. Shift should be lies within (t+ (0517t) & (t-1) at que limit. to = 1. here, 1 + (OSTT = 1-1=0. Cost. M(F-3), 8(F-1) qt = 0. 2 wit -3) ०५९४१५०. **γ**(0 S(4-1) Ans is o. ςο, uct-3). 8(t-1)=0. x(2-t). \$(4-t) dt. 8 (4-t)= 8 (t-4) (-...8(t)=8(-t)). so, to=4. = x (2-to). x (2-4) x(-z).

$$\bigoplus_{SOIN} \begin{cases}
6 & 5 & (3t-9) \cdot dt
\end{cases}$$

$$= \frac{1}{3} \cdot e$$

$$= \frac{1}{3$$

()

=> The function which do not Posses higher V desirative use singularity br. e.g. 8(t) & U(t). bunction: Signum u(t) W(-t) -u(-t) =) For any odd b" ampiitude is zero at oxigin. Sign(t) = u(t) - u(+) Sign(t) = 2u(t) - 1u(t) + u(-t)=1 for t=0. only. L→ Exponentials: (Tt) Q Real exp. e. (,)

7,00t Complex sinusoid

GXD. Complex

$$f(\omega i + y) = e^{(\tau + i\omega)} t$$

$$\frac{1}{2}$$
 $\frac{1}{3}$ $\frac{1}{4}$ $\frac{1}{2}$ $\frac{1}{3}$

$$u(n) = 1 ; n > 0$$
 $= 0 ; n < 0$

()

 \bigcirc

([])

()

5 (X)

⇒ It is not a Sample Vession of 21(t). because u(t) = discontinuous at t=0.

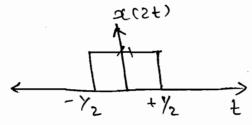
$$\nabla x_n = x_n - x_{n-1}$$

$$u(t) = \int_{-\infty}^{\infty} 8(z) dz$$

$$u(n) = \begin{cases} x \\ x \\ -\infty \end{cases}$$
 put

m= 00 u[n] = \(\S[n-m]. \) W2 0

$$\Rightarrow x(2t)$$

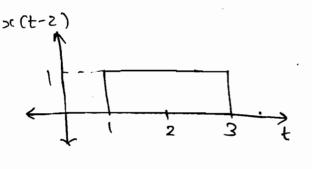


$$x(2t) = 1$$
; $-1 < 2t < 1$
 $x(2t) = 1$; $-\frac{1}{2} < t < \frac{1}{2}$

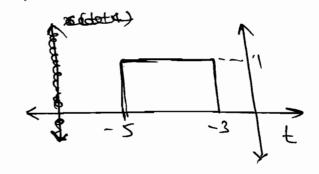
()

٦

()



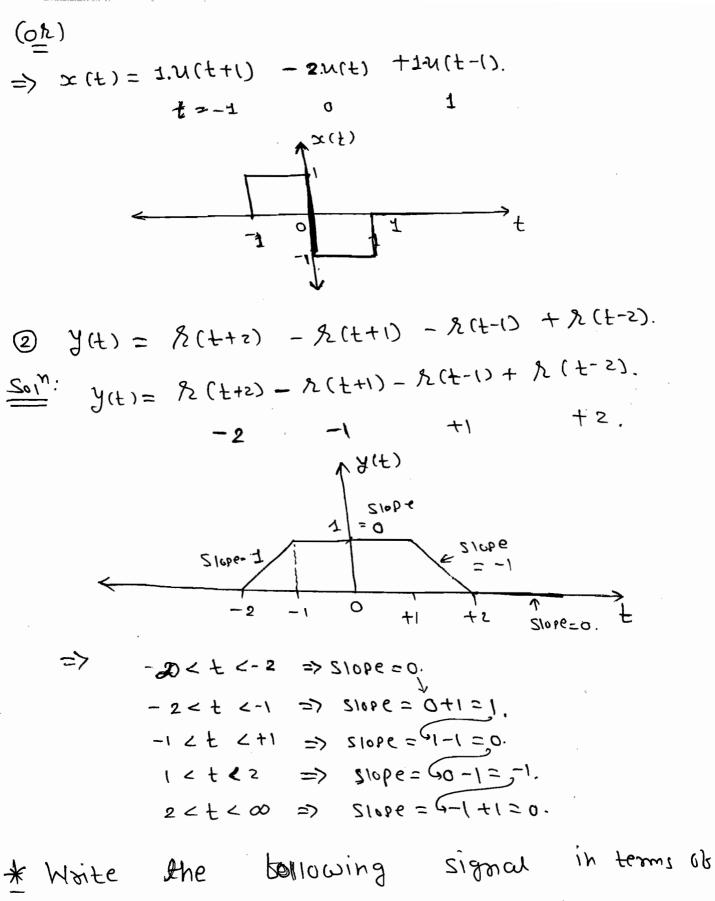
(ii)
$$x(t+4)$$



- -> Right Shift
- -) Time delayed

t. < 0)

=> In Real-lime, time und vance is not possible. i.e. we can not predict any output before giving a input. [0-1] Doaw the bollowing signals: O u[sinTt]. SINTLE > 0 Soin: u[sinTt] = 1; = 0 ; SINTITE < 0. FITMIZ A $\langle \cdot, \cdot \rangle$ AU(+1) Soin: -2W(t) u(1-1)



 $(\dot{} \dot{} \dot{})$

(

(9

 \bigcirc

 \bigcirc

(-)

 \bigcirc

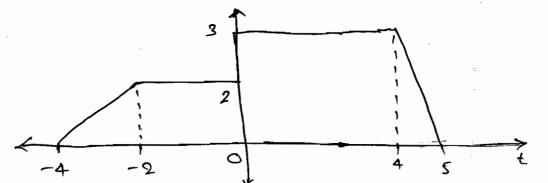
(]-

0

<u>(</u>

();

Singularity bus:



$$\frac{Soi^{n}}{2}; \quad y(t) = 1.8(t+4) - 1.8(t+2) + u(t) - 38(t-4) + 38(t-5).$$

Sol):
$$\lambda(t) = \frac{1}{5} \lambda(t) - \frac{1}{4} \lambda(t-1) + \frac{1}{5} \lambda(t-1)$$

0

- $0 \propto (1-t) + x(s-t) = 0$ by t = 8
- ⑤ x(1-f) x(5-f)=0 Poy f €

$$x(1-t) = 0$$
; $1-t < 3$
 $x(1-t) = 0$; $t > -3$

$$\Rightarrow \quad \chi(2-t) = 0 ; \quad 2-t < 3$$

$$5c(2-t) = 0$$
 ; $t > -1$.

* For the signal x(t) shown in figure.
Douch the boldwing signals:

(

(...

()

 \bigcirc

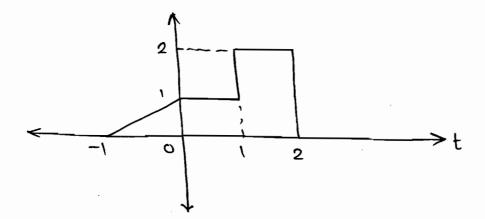
O

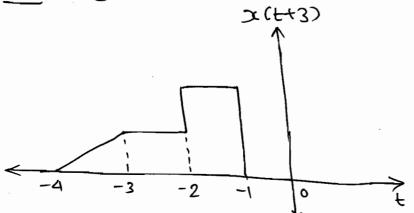
(

(:

()

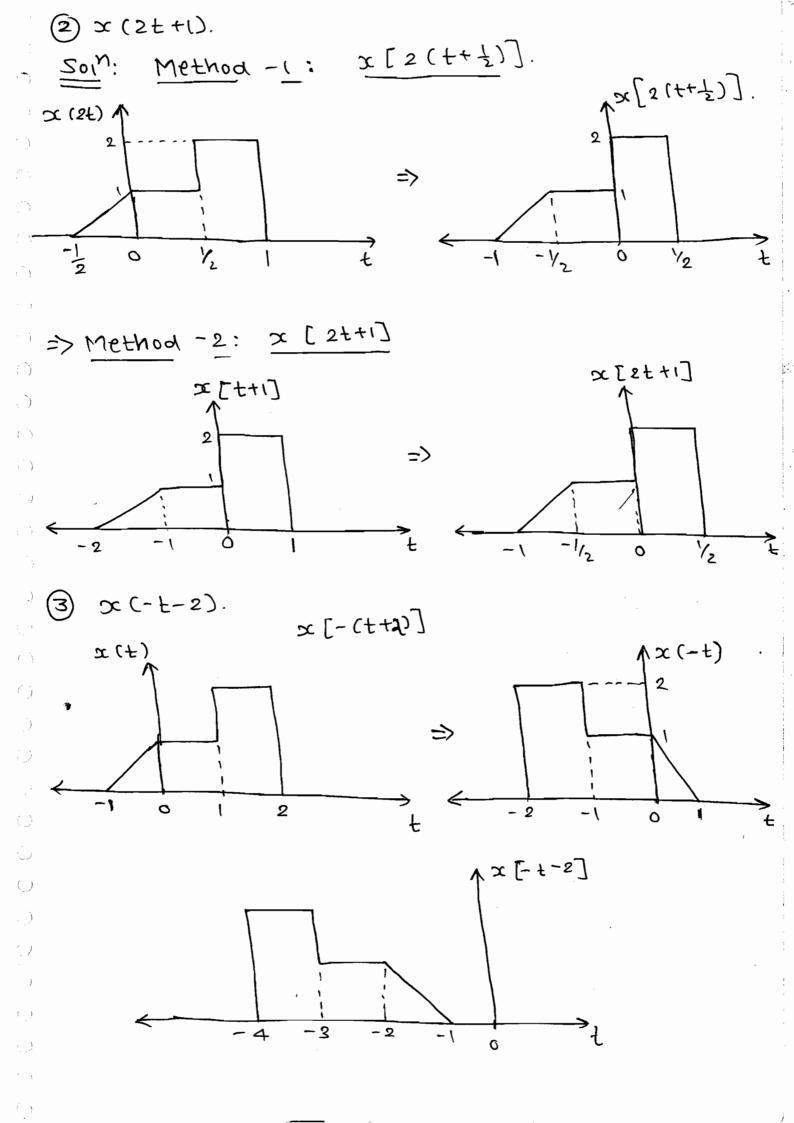
 \bigcirc

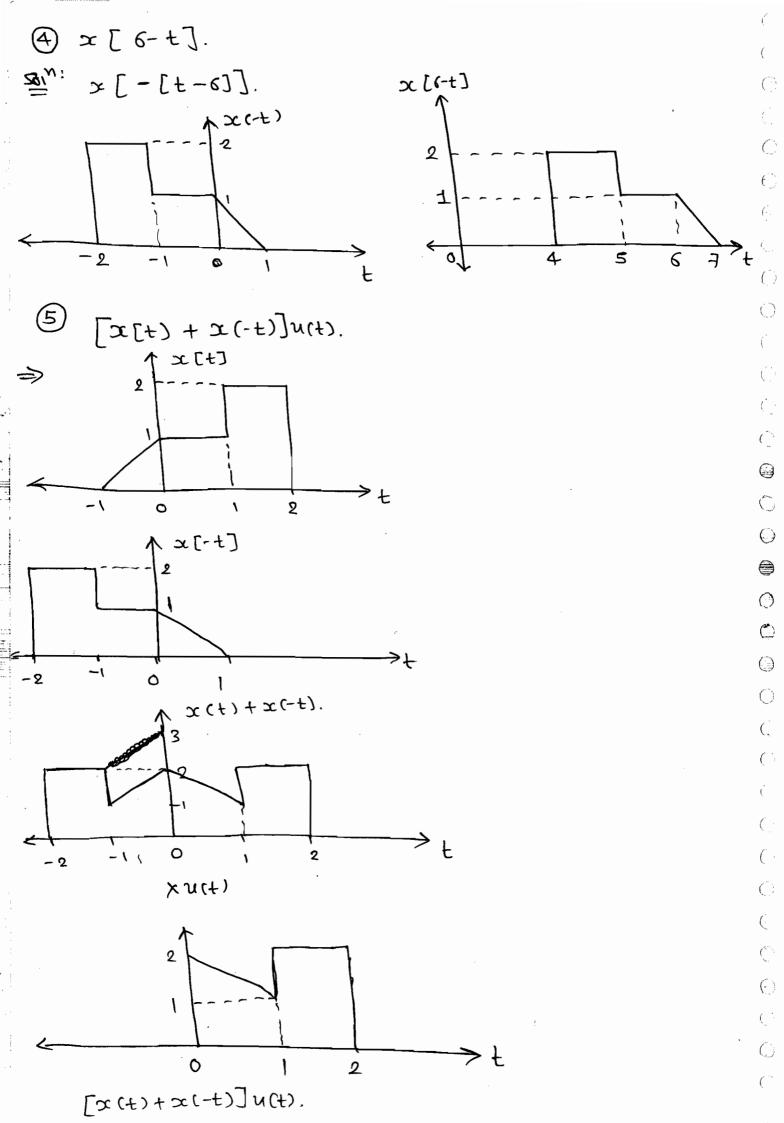




$$\Rightarrow$$
 Method: -0 : $x(t) = x(\alpha(t + b|\alpha))$.

$$x(t) \longrightarrow x(t+b) \longrightarrow x(at+b).$$

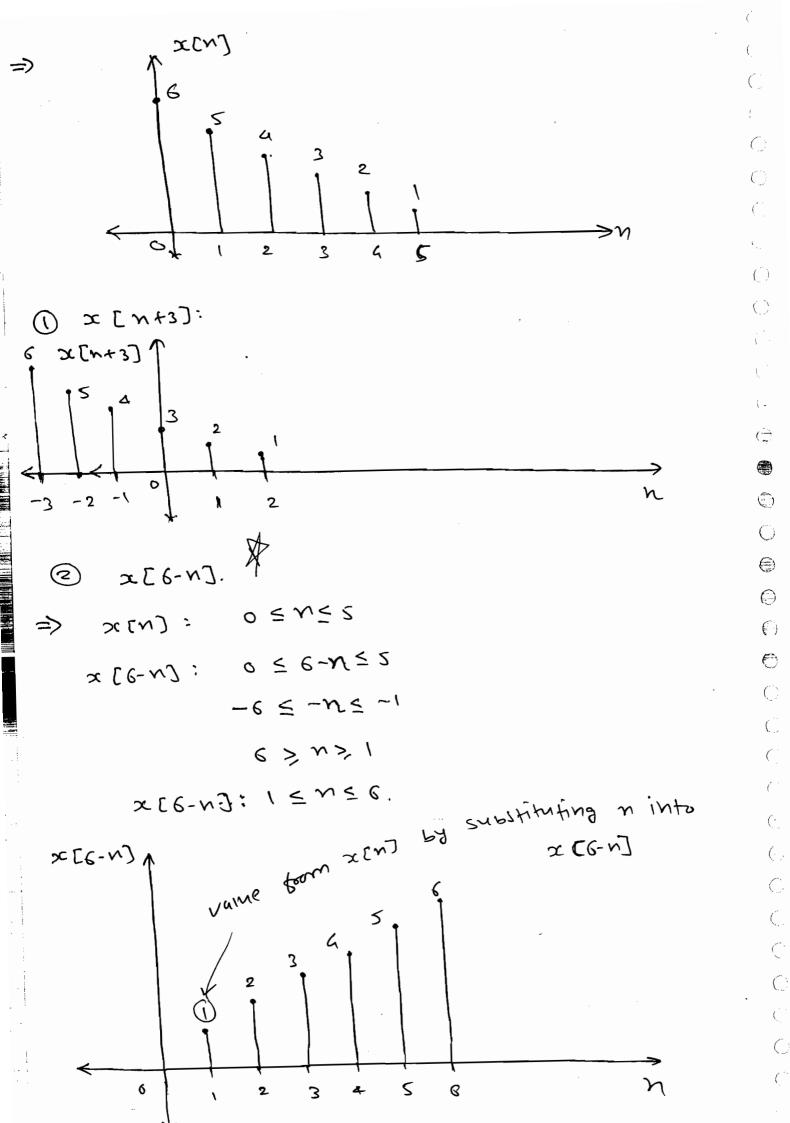


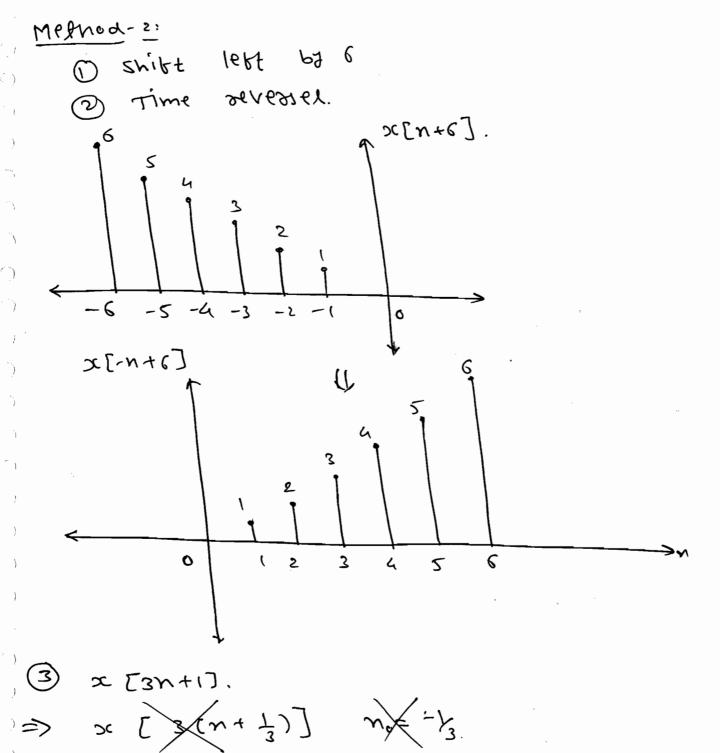


*
$$\times (1-t(3)) = \times [-\frac{1}{3}(t-3)].$$

$$\Rightarrow \times (t) \xrightarrow{\text{T.R.}} \times (-t) \xrightarrow{\text{T.S.}} \times (-t(3)) \xrightarrow{\text{R.S.}} \times ([t-3)-\frac{1}{3}].$$

$$\Rightarrow \times (t) \xrightarrow{\text{Can}} \text{ be} \xrightarrow{\text{Can}} \text{ be} \xrightarrow{\text{T.M.}} \times (-t(3)) \xrightarrow{\text{T.M.}} \times (-t$$





MOTE: Method-I i.e. bisst scaling and then shifting may be bails in discrete + domain. because n is integer. So, always go though by bollowing two methods.

Method $-\underline{\mathbf{I}}$: $\propto [3n+1]$: $0 \leq x \leq 5$. $-4 \leq 3n \leq 4$ $\therefore -\frac{1}{2} \leq x \leq 4/3$.

M46x, Vuild $-0.33 \leq m \leq 1.33$. but n is unways integer. So, vaid n in sunge (-0.33, 1.33) n=0 & n=1. is XE3X +1) Method-II: > 1) shibting 2) scaling. FW3 XA 3 x[3nt1]一岁, 0, 岁, 岁, 少多 5

 \mathbf{C}

 \bigcirc

()

Ć.,

<u>(</u>

 \bigcirc

e O

C

1.

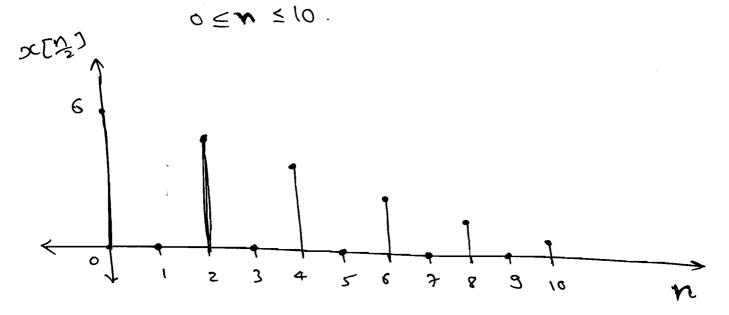
(4) $x [\frac{N}{2}]$ $\Rightarrow x (N): 0 \le N \le 5$ $x [\frac{N}{2}]: 0 \le \frac{N}{2} \le 5$

1)

.)

 $\dot{})$

__)



* Interpolation and Decimation.

=> In cont lime domain,

x [at] -> Scaling Property,

a is scaing tactor.

if a>T => Combrezzion

ac1 => Expanssion.

=> In Rom discrete lime domain,

x [mn] -> scaling Preperty.

if m>1 => Decimation.

m<1 => Interpollation.

=> In above example, we can say

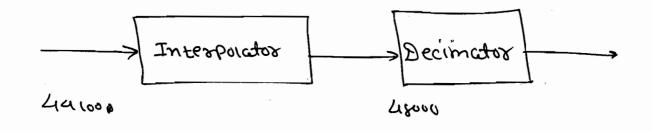
Zeso- interpolation because it makes som

Sumple Zero.

=> Multi-Rate DSP.:

=> C.D.: fs = 44.1 KHZ.

D.A.T .: 3 = 48 KHZ.



fs,: 32KHZ

352: 48 KHZ.

NOW, WE WANT to CONVERT 32K KER S.R.

to the 48 K S.R.

$$\frac{48}{32} = 3l_2 \Rightarrow x\left[\frac{2}{3}n\right].$$

NOTE:

=> Conversion of one sampling rate to another sampling rate is multirate DIP which is done by using decimator and ()

 $(\dot{})$

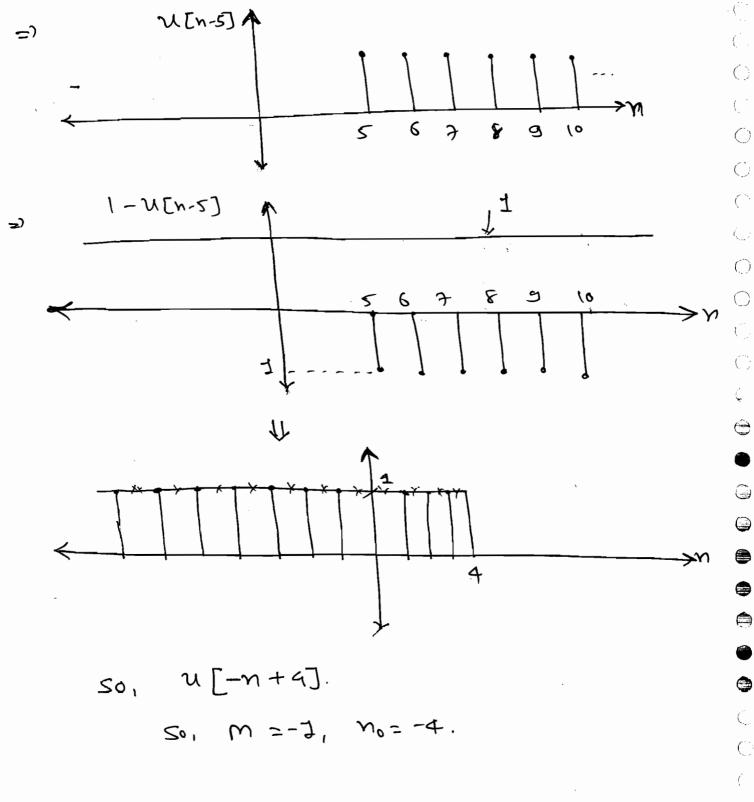
 Θ

 \bigcirc

 \bigcirc

 \bigcirc

interpolation. -> whenever we want to perform this Operations simultaneously birst do Interpolation and then Decimation. (Down Samping). Cup sampling) i.e. it x [axi] -> then bisst do x [xi] and then x [an]. > In interpolation no. 06 samples increases and in Decimation no. 06 samples Decrewes. 5 sc[n-1] 8[n-3]. => x [n-1] 8 [n-3] No= 3. :. by sibting preperty ob 8 x[3-1]. 8[n-3]. = 41.8[n-3]. $[\alpha]$ If $x[n] = 1 - \sum_{k=4}^{\infty} S[n-1-k]$. Such that x[n] = u[mn-no] find M 4 No. U 5617: x[n]= 1-[8[n-s] + 8[n-6] + 8[n-7]+...]. x[n=1- n[n-5]

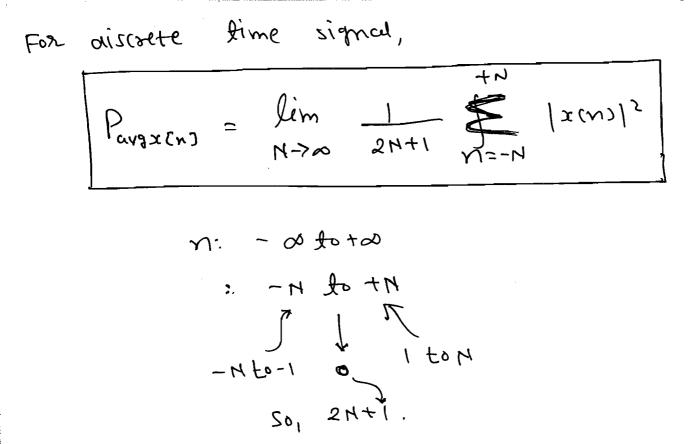


 \bigcirc

 \bigcirc

 \tilde{C} .

	Classification ob signas: $\Rightarrow x(t)$.
	Energy and power signal:
⇒ ->	Energy signal:
^ →	It Energy of a signal is finite then
1	it is called Energy simp signal i.e
) →	For cont time signal,
() () ()	$E_{xct} = \lim_{T \to \infty} \int xct ^2 dt. = tinite.$
	For discrete time signal,
(*) (*) (*)	$E_{x[n]} = \lim_{N \to \infty} \frac{N}{N^{2-N}} = binite.$
	For Complex $ x(t) ^2 = x(t).x^*(t)$.
()	Power signal:
	It + power of a signar is finite i.e.
0	o < p < or then it is called power signal
(,) (,)	Parace = lim 1 sect) 2. at.



=> The Physically Possible (0%) Poactically
possible signal is said to be the
Energy signal it tollowing Conan is

Satistica:

As
$$t \rightarrow t\infty \Rightarrow t \rightarrow t \Rightarrow t$$
 Energy signal

 \bigcirc

()

(F)

 (\cdot)

€

 \bigcirc

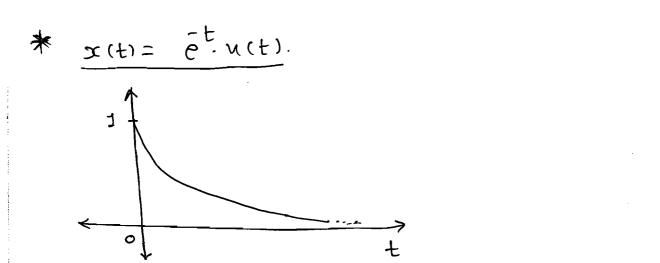
(:

 \bigcirc

 (\cdot)

()

 \bigcirc



$$= \lim_{T \to \infty} \left[\frac{e^{-2t}}{T} \right]_0^T$$

$$= \lim_{\tau \to \infty} \frac{-2\tau}{2}$$

.)

$$=\frac{1}{2}$$
. = finite,

So, Energy Signal.

$$P_{av} = \frac{1}{T - \infty} = \frac{1}{\infty} = 0.$$

So, An Energy signal Should has Zeroo avg. Power.

-> over the signal is existing it Should maintain the binite amplitude level.

$$\frac{*}{2} \quad \frac{3(t)}{t} = \frac{1}{t} \frac{1}{t}$$

=> at t=0 its amplitude is ∞.

=) at t= 00 it's amplitude is ZERO.

so, this type of signal ann't be generated.

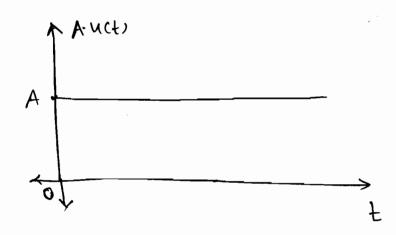
=> Power signal:

=> A signal which maintain constant

amplitude over infinite time is a

power signal.

e-g. y(t) = A·u(t).



Par = 11m 1 1 A2-dt

 \bigcirc

()

 \bigcirc

ί.

 \bigcirc

9

()

0

()

(`.`

 \bigcirc

Par = im 1 x A? T.

 $= \lim_{T\to\infty} \frac{A^2}{2}.$

$$P_{av} = \frac{A^2}{2}.$$

MOW, Par = im 1 E.

=> E = iim 2T. (Pay).

E = im 2T. A2/2

$$E = \infty$$

=> So, Power signal require on every.

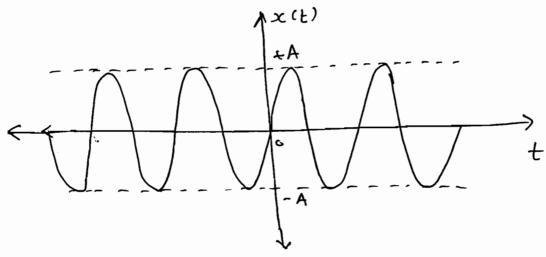
=) The signal Cannol be both energy and power signal Mutually Exclusive.

=> Au periodic signals are power signals

because they maintain constant amplitude

over a infinite time.

for. e. a. (i) x(t) = A (o) (ω, t+0).



$$P_{av} = \left(\frac{A}{\sqrt{z}}\right)^2 = (Rms)^2 = (mean square)^2$$

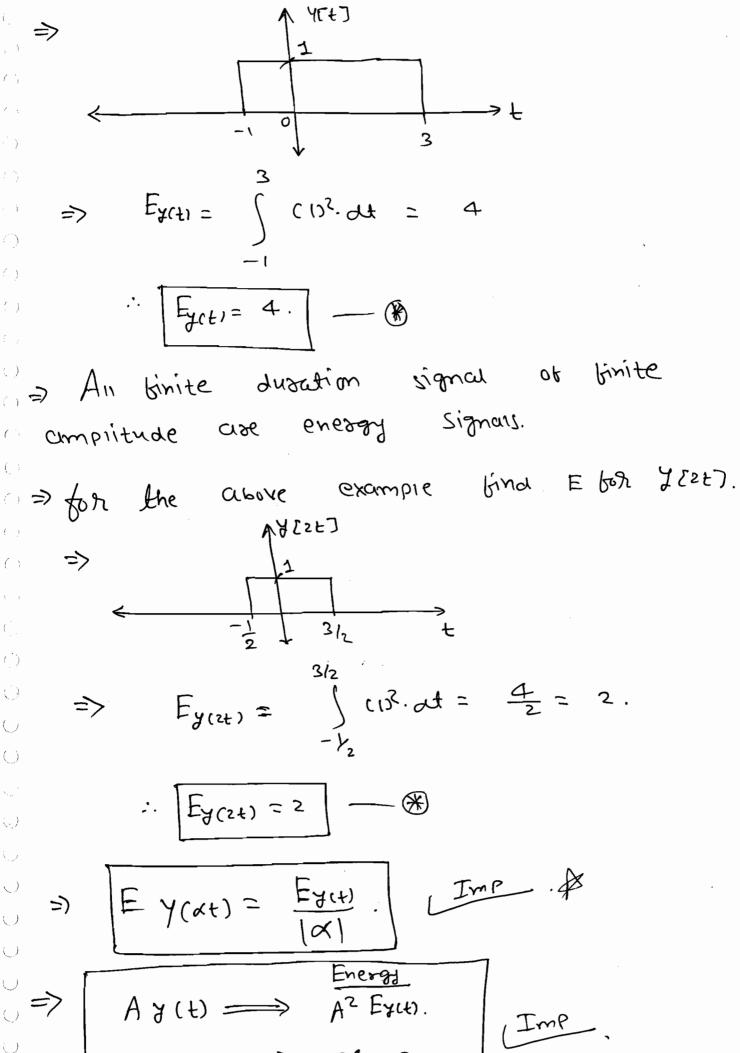
=
$$\lim_{T\to\infty} \frac{1}{2T} \int_{-T}^{T} A^2 \cdot \left| e^{j\omega_0 t} \right|^2 \cdot dt$$

=> Comprex simusoidal is also a power signal.

=> What is Nature of signal below: 1x(4) So, Energy Ae^{-t} at t->0 Power (: Grit. Amp.) $\Rightarrow P_{\alpha \nu} = \lim_{T \to \infty} \frac{1}{2\tau} \int |x(t)|^2 \cdot dt.$ = 1im _ _ A2. 62+] A2. 62+] . dt. 1 S A2. dt Esimalhas zero 27 S Power Su power +u= power -T Case-(ii) it & signed then Phas infinite E. so, E=00 means as E-100 =)E-100 Power + Energy = Power. [] If x[t] = 8(t+1) - 8(+-3). Find the $\forall C+J = \int_{-\infty}^{\infty} x(T)dT$ in J(t) =) (8(++1) - 8(+-3)) dr. = U[++1 - U[+-3]. = u[t+1) - u(t-3),

(

 \odot



A+7(1) => 0=E Power + Energy = Power

=>

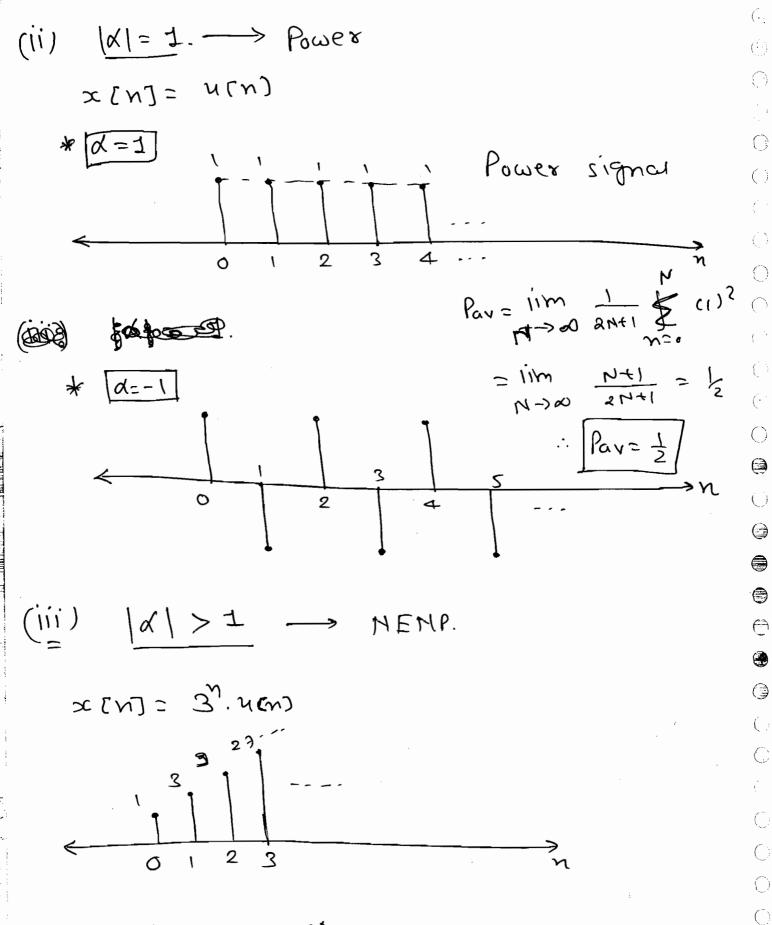
For x(t) = 2(t) - 2(t-1). 566 po wers constant (amp. Enersy very by Fig =) AM=U.(Energy + Power = Power. 6 -41.45 * $= 11) \times$ ٥ +00 Signal Energy occti= tuct). => t>0=> Amp ->00 SO, NEMP.

(7

* A(F)= Az+->-0 A(4) Amp -> 0. So. N.E. N.S. To make Energy signal, Comp at $t \rightarrow -\infty$ & must be zero. $t \rightarrow +\infty$ Note: => Cont' Impuise function is N. F. M. P. signal, => Discrete impulse is Energy signal. * Discrete Signal: => > [n] = 2 n u [n]. (i) For IXI<] Energy. x[n] = (1)n, u[n].

So, Energy signed.

C) $t \to \infty \Rightarrow cmp = 0$.

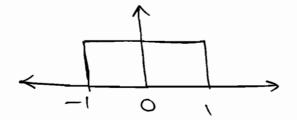


As $N \rightarrow \infty$ $amp \rightarrow \infty$ 50, N.E.N.P.

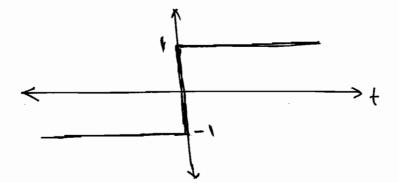
 \bigcirc

(

$$\Rightarrow$$
 $x(t) = x(-t)$.



$$\Rightarrow$$
 $x(t) = -x(-t)$.



Even Conjugate:
$$x(t) = x^*(-t)$$
.

$$x(-t) = t^2 \cdot e^{-j\omega t}$$

$$x^*(-t) = t^2 \cdot e^{j\omega t} = x(t)$$

$$\Rightarrow 0dd \quad \underbrace{(onjugate:} \\ x(t) = -x^*(-t).$$

$$for. \quad e.g.: \quad x(t) = t \cdot e^{-t}.$$

$$\Rightarrow x(t) = x_e(t) + x_o(t). \quad -(t).$$

$$Replace \quad \dot{t} \quad bd \quad \dot{t}$$

$$\therefore x(-t) = x_e(-t) + x_o(-t).$$

$$\Rightarrow x(-t) = x_e(t) - x_o(-t) - (T).$$

$$\Rightarrow form \quad ear \quad (T) \quad e \quad (T).$$

$$\Rightarrow x_e(t) = x(t) + x(-t)$$

$$x_e(t) = x(t) - x(-t).$$

2

()

()

(

(

 $(\dot{\cdot})$

()

(=)

 $(\dot{\cdot})$

()

(1)

 \bigcirc

()

(; /

(i

· ·

(. .

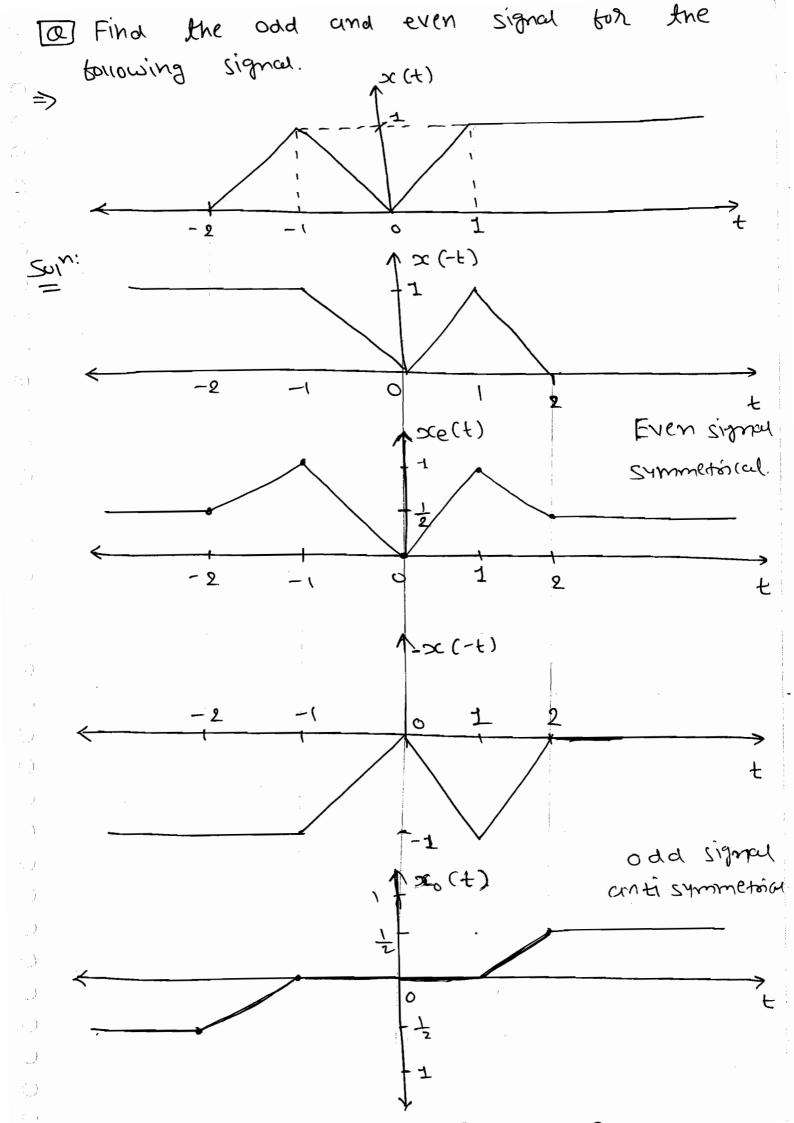
()

(;

0

()

(_. .



$$\Rightarrow A_{8}eck \quad wider \quad even \quad signal:$$

$$\int_{-q}^{q} x_{e}(t) dt = 2 \int_{0}^{q} x_{e}(t) dt.$$

$$\Rightarrow A_{8}eq \quad wides \quad odd \quad signal = 2eso.$$

$$\Rightarrow e+e = 0 \qquad e\cdot e = e$$

$$0+0 = 0 \qquad 0 \cdot 0 = 0$$

$$e+0 = veno \qquad e\cdot 0 = 0$$

$$e+0 = veno \qquad e\cdot 0 = 0$$

$$\Rightarrow \frac{d}{dt}(e) = 0 \quad e \quad \frac{d}{dt}(o) = e.$$

$$\Rightarrow \int_{0}^{q} (e) dt = 0 \quad e \quad \int_{0}^{q} (e) dt = e.$$

$$E_{x(t)} = E_{x(t)} + E_{x(t)} = E_{x(t)} + E_{x(t)}$$

$$= \int_{-\infty}^{\infty} \left[x_{e}(t) + x_{o}(t) \right]^{2} dt.$$

$$= \int_{-\infty}^{\infty} x_{e}^{2}(t) dt + \int_{-\infty}^{\infty} x_{o}^{2}(t) dt + 2 \int_{-\infty}^{\infty} x_{e}(t) x_{o}(t) dt$$

Etotal = Eeven + Eodd.

٠

[a] The Conjugate Antisymmetric part of
$$x(n) = \{ (+i)2, 2, 14 \}$$
.

Solve $x_{oc}[n] = \frac{x(n) - x^*[-n]}{2}$
 $x_{oc}[-i] = \frac{x[-n] - x^*[i]}{2}$
 $x_{oc}[-i] = \frac{i+i6}{2}$

Similarly, $x_{oc}[0] = \frac{x(0] - x^*[0]}{2} = \frac{3-3}{2} = 0$.

 $x_{oc}[1] = \frac{x[1] - x^*[-1]}{2} = \frac{i4 - (+i)^2}{2}$
 $x_{oc}[1] = \frac{-i+i6}{2}$
 $x_{oc}[n] = \{ \frac{(+i6)}{2}, 0, \frac{-1+i6}{2} \}$.

[3] Periodic & Non-Periodic Signal.

 $x_{oc}[n] = x(k+1)$

The Leust Period of $x(t)$.

Solvi (1)
$$\omega_1 = 50\pi$$
?
$$\frac{2\pi}{T_1} = 50\pi$$

$$\frac{2\pi}{T_2} = 60\pi$$

$$T_2 = \frac{1}{30}$$

$$\frac{T_1}{T_2} = \frac{30}{25} = 615$$

$$= S \times \frac{1}{25}$$

$$T = \frac{1}{5}$$

(

()

()()

 Θ Θ Θ

() (<u>-</u>

0 0

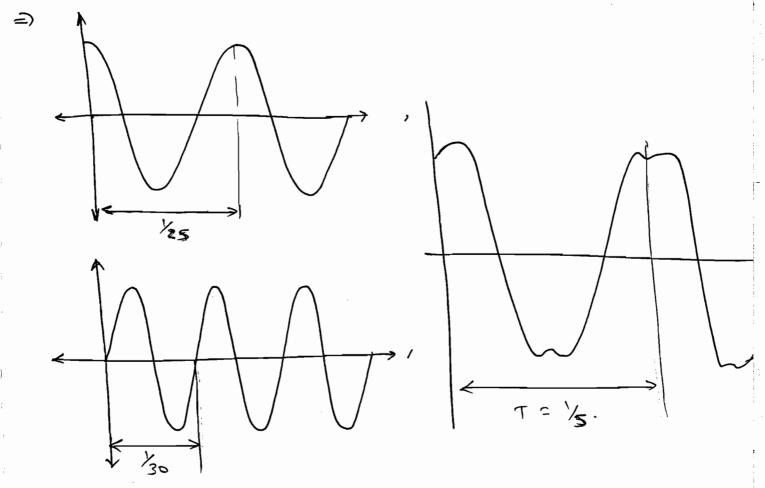
(;

(

(:

0

0



()

$$TOI = 0$$

$$\frac{2\pi}{T} = 10\pi \Rightarrow \boxed{T = \frac{1}{5}}$$

$$= \frac{T}{6} = \omega_0 \Rightarrow \frac{2\pi}{T} = \frac{\pi}{6} \Rightarrow T=12$$

$$J(t) = \frac{1}{2} \sin\left(\frac{227Tt}{15}\right) - \frac{1}{2} \sin\left(\frac{27T}{15}\right).$$

 (\cdot)

 (\cdot)

$$\therefore \quad Cr(O\left(\frac{22\pi}{15}, \frac{2\pi}{15}\right).$$

$$=\frac{15}{211}=\omega_0$$

$$\Rightarrow \frac{2\pi}{T} = \frac{2\pi}{15}$$

$$T_1 = \frac{2}{13}, \quad T_2 = \frac{2\pi}{13}.$$

So,
$$\frac{T_1}{T_2} = \frac{17}{12\pi}$$

Troational

brase andre of 30. => Additional $\Rightarrow j = e^{j\pi l_2}$ It never changes periodicity. \Rightarrow $\omega_0 = 10 \Rightarrow T = \frac{2\pi}{15}.$ $\int C(ot + \frac{\pi}{5})$ 6200P ; y(++ ∓) = j. e 110t 12TT = j·e · = j.e ((0) 277 + isiher) ·. y(++ 丁) = y(+) レ - (54j3)f =(D) $x(t) = e \cdot e$ S017: Mon-periodic periodic. y(t) = sin (IIt). u(t). 201,: >t > Non-Periodic An pessodic signant alse Sin(#) + u(+). everlaiting signal = - ato thre;

$$= \frac{x_{e}(+) = \frac{(0)3777 \cdot x(4)}{2} + \frac{(0)377(-4) \cdot x(-4)}{2}$$

()

()

()

(<u>J</u>)

()

 (\cdot)

 \bigcirc

()

Ö

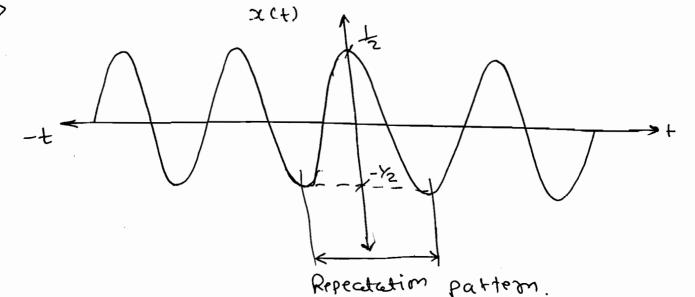
(

()

(·)

:.
$$x(t) = \frac{\cos 3\pi 7}{2} [u(t) + u(-t)].$$

$$u(t) + u(-t) \Rightarrow \frac{1}{-t}$$



$$\frac{1}{2}$$
 $x(t) = \frac{\sin 3\pi t \cdot u(t) + \sin 3\pi (-t) \cdot u(-t)}{2}$

[uc+1 - u(-+)]. SIN 3117 $\propto Ct1=$ u(t) -u(-t). +) Mon-Pessodic. So , S (-1)k. 8(t-2K). J(+)= + 8(f+5) + 8(f) - 8(f-5) y (t) + 8(t-4) + --. Repeating T=4 sec. Sul begodic 1=45

 $A = \sin \left[\frac{3\pi n}{2}\right]$ Continuous sinusoids and Complex Zinnzoige are beriodic for Energ Vuine 06 wo whereas the equavalent discrete terms use Periodic it $\frac{\omega_0}{2TT}$ is a Rational Number $\left(\frac{m}{r}\right)$. => To make N as the time Period signal, m no. of buil (yeles confinuous signal is repeated. x[n] = x[n+N].

x[n] = Sinwon!

=> x[n+n] = sin ch (n+n].

= $\sin \omega_0 n$. $\cos \omega_0 n$ + $\cos \omega_0 n$. $\sin \omega_0 n$.

():

(·.

(

 $(\dot{})$

()

()

زی)

(=)

۱

()

()

(

(

0

=> (01 WIN = (02 SILLW = 1. for m = 0, +1, +2)...

: WON = 2TM.

 $\therefore \frac{\omega_0}{2\pi} = \frac{m}{N}.$

$$\frac{\omega_0}{2\pi} = \frac{3}{10} = \frac{m}{N}$$

2)
$$\times [N] = (0) \left[\frac{N}{6} + \frac{\pi}{4} \right].$$

$$\frac{1}{201}$$
 here, $\omega_0 = \frac{1}{6}$.

3
$$\propto (n) = \sin\left(\frac{\pi n}{3}\right) + \cos\left(\frac{\pi n}{4}\right)$$

F → CCU.

 $(4) \quad x(t) = 2 \cos \left(150117 + 45^{\circ} \right). \quad 1 \quad f_s = 200 \text{ Hz}$ $(50)^{n}. \quad \text{Convert} \quad \text{Cont}^{n} \quad \text{to descrete} \quad \text{by}$ $\text{put } \quad t = nT_{5}.$

(.

()

0

()

()

()

(3)

()

(_:

$$\therefore \times [nT_i] = 2 \cos \left(150\pi n \cdot T_i + 45^i \right).$$

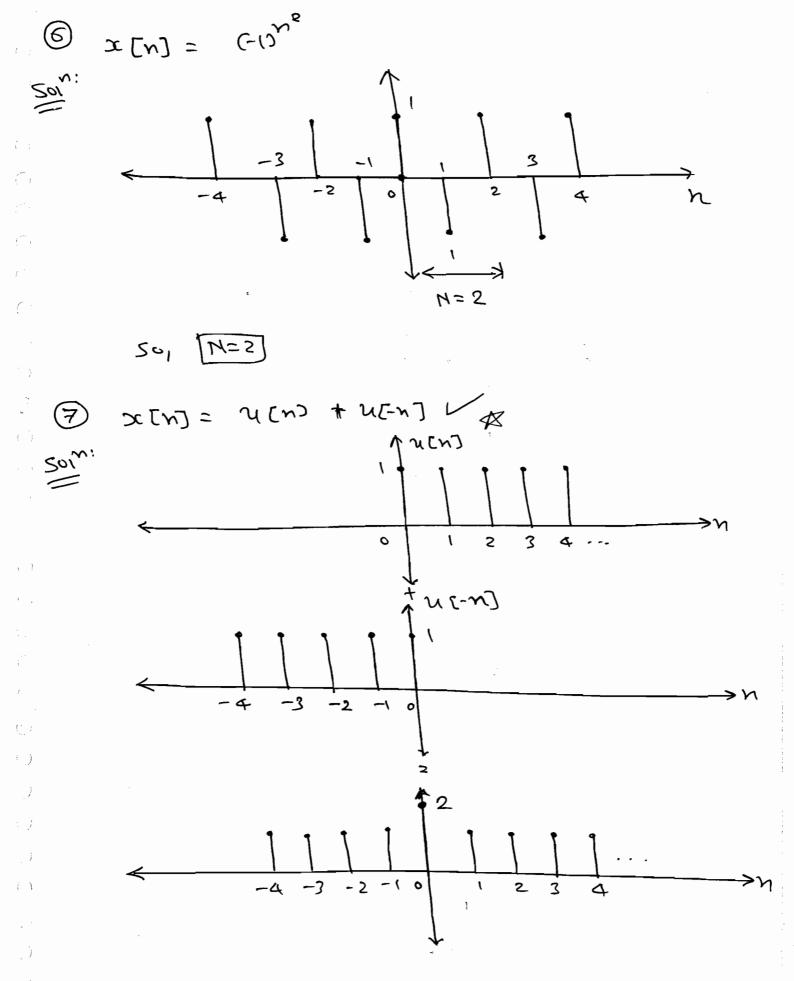
$$\Rightarrow$$
 $()_0 = \frac{150\pi}{200}.$

$$\therefore \frac{2\pi}{2\pi} = \frac{15}{20} \times \pi \times \frac{1}{2\pi} = \frac{318}{20}$$

$$(i)^{\infty} \propto [n] = (i)^{n/2}.$$

$$\sum_{z \in J_{z}} x [\omega] = e \qquad (\therefore j = e_{\overline{j}}).$$

$$: \frac{\omega_0}{2\pi} = \frac{\pi}{4} \times \frac{1}{2\pi} = \frac{1}{8}.$$



So, non - Periodic.

[8] 8[n-3k] - 8[n-1-3k]. $= (n) \times$ K=-00 + 8[n+3) - 8[n+5] 5017: = [N] = + S(m) - S[m-1] + S[m-3] · · · + [4-m] 3 -CNJx5 3 2 N=3 signais: (ansal Lanson & Non-Cansal: Betined for the time only. t >0 (on) かその. => 6.2x(+)= 0; f<0 x[n] = 0; x < 0. 1) x(t1= u(t-1). Causal

 \bigcirc

 $(\)$

 (\exists)

(-)

0

 \bigcirc

(,

()

(:

(...

0

(

()

(.`

② y [-t-i] = ~[-(++i)]. Anti-Causa 3 Non- Cansal NoFe: => A11 (ausal signals are Right sided signer, but ar signt sided signer may (08) may not be Causa signal => Right - sided: (t>to) Rignt-sided Rignt -sidea Non- Consa Canicy. <u>Lekt</u> - <u>sided</u>: (t < to).

signais are Power Periodic and Random signor. But Aperiodic and Deterministic simals may (on) may not be energy signal. uct) -> is non-periodic and it is power-signed. * Houbet: => By approximating a unit area friungular function we can generate unit impulse br. In a simillar manner bit (-)approximating desirative of triungular Produce doublet. (8°(+)). => [Area under Doublet is Zero.] Slope = $\frac{1}{7^2}$ $\frac{1}{7}$ $\frac{1}$

$$\Rightarrow \frac{\text{Sitting}}{t_2} \frac{\text{Prepenty:}}{x(t)} = \frac{t_2}{x(t)} \cdot \frac{t_1}{x(t)} \cdot \frac{t_1}{x(t)} \cdot \frac{t_2}{x(t)} \cdot \frac{t_1}{x(t)} \cdot \frac{t_2}{x(t)} \cdot \frac{t_$$

Desirative ob Doublet is Tomplet and we Should Consider parabolic curve instead ob triungular curve since triplet is double desirative ob impulse. Double desirative ob Parabolic curve is unit step trunction.

= 400

Systems: => 910 11P excitation Response. =) C.T.S. A(F) x(f)T-{·} y(1) = ~ (x(+)). e-g. y(+)= lnx(+) $= x^{2}(t)$. Systems => Synthesis. Designing ⇒ Anaiysis. Am Getting 0/6 Dibberentica en Difference en T.F. model State H(3) / H[m] Space Impulse Response hct) | hcm]

()

()

(.

()

()

()

()

(...

()

£::::

€

 $\overline{}$

()

()

()

(:::

 \bigcirc

3	Lineur,	Stable,	Investible	-> Considering
		,		Amp.

$$\mathcal{D}_{1}(t) \xrightarrow{T} \mathcal{Y}_{2}(t)$$

$$\mathcal{D}_{2}(t) \xrightarrow{T} \mathcal{Y}_{2}(t).$$

$$\Rightarrow$$
 $\forall x(t) \longrightarrow \forall y(t).$

e.g. y(t) = x(t).x(t-3).

$$x(t) \longrightarrow X(t) = x(t). x(t-3).$$

$$\chi_2(t)$$
 \longrightarrow $\chi_2(t) = \chi_2(t), \chi_2(t-3),$

$$y(t) = (x(t) + x_2(t)) \longrightarrow (x(t-3) + x_2(t-3))$$

 $\boxed{Q} - \boxed{1} \qquad \forall (f) = x(f) \cdot (ossf)$ $x(t) \Rightarrow y'(t) = x'(t)$, coist. $x_2(t) \Rightarrow y_2(t) = x_2(t)$. (o) 5t. => x(4) + x2(4) => J(t)= (x(4) + x2(4)) (0157 = x(t). (o)St + $x_2(t)$. (o)St y(+)= x(+) + y(+) => Lineur. Unknown signal product make the System non-lineurs. $y(t) = \int x(T) dT$ -00 L

()

()

 Θ

 \bigcirc

0

()

 \bigcirc

0

()

(...

2 Linear. =>

- 3) y(t) = Sumple {x(t)}.
- System operation is sampling, =>

___ Amplitude is not Changing So, Linear.

Sampling is a linear operation, but time dependent (Ts) so, time Vusignt.

3) y(t) = sin {x(t)}. Non-lineur Jict) = sin (x(t)), Joct) = sin (x(t)). 0 So 1/2; (H) => sin (x,c+)+ x2(H) = sin {2(4)} + sin {2(24)}. <u>Note</u>: When old is toignomatric bunction System is always Non-Linear. (+) (+) = (m(+) Son: Non-linear > All tre values becomes - Ye vames O[P] due to -5x(4) = [-5x(4)] = 5[x(4)].dy(+1= -5 (x(+)) + 5 (x(+)) So, Non-lineur. Mote: Modulas ob ilp makes the system Non-lineur. be cause au tre values, becomes the Vaine. (3) y(t) = 3x(t) + 3...Soin: Non-linear OIP due to dy(t) = d(3xct) + 5).

= 3 xx(+) + 5 x'

```
= 3 dx(H) + T.
     So, Mon-linear.
                                               \bigcirc
     Addition of Constant makes the
Note:
                                               ()
       System Non-linear.
                                               (:
     This system is also called or
                                               ()
     Incoemental Lineur "since OIP is
                                               ()
   increasing because of constant term.
                [N]x
6
     2 = [N] X
                                               ()
                                   22
                54 (W)
                                               , 7 (M) = 2
50171:
       y(εn) = 2.
                                               ()
                                               (\hat{z})
    : old que to sa[m] + x2 [m]
                                               x(n) x(n)
                                               \bigcirc
                    2 .
                              X2(M)
                                               \Box
                    x(m)
                                               (\hat{\cdot})
                <del>+</del> 2 +
       So, Non-invert.
                                               (...
      Exponential terms makes the system
Mote:
       Mon-Linear.
7
     Y(m) = Som [x(m)].
     y[m] = 1; x[m] >0.
          = -4; x(x) < 0.
```

old que to & suct)

So, Mon-linear.

=> For signam we are always maintaing Const. amp ob ±1. so it is non-linear.

Mote: When old signal is input dependent then it is always Non-Zinear.

[8] Y[n] = x*[n].

 501^n : old the to $(2+j3) = \{(2+j3) \times (2n)\}^*$.

 $= (2-j3) \cdot x[n]$

d x [n] = (2+i3).x[n] = + Non-liheur.

[G] Y (N) = Real [>UM)].

5017: OID due to 2+13 = Real (2+13).x[m].

= 2. Real [I[n]].

(2+i3) Real [x[n]] + 2 Real [x[n]].

Su, Mon-linear.

Note: → Real, Complex pura and Consugate

au are Non-linear.

[[o] &[n] = median [x cm].

 $\frac{501^{12}}{501^{12}} = \frac{1}{11} \frac{1}{11} \frac{2}{11} \frac{1}{11} \frac{1}{11} \frac{1}{11} \frac{2}{11} \frac{1}{11} \frac{1}{11} \frac{1}{11} \frac{1}{11} \frac{1}{11} \frac{1}$

op, + op₂ = $\frac{1}{2}$ | 1, 1, 1, 1, $\frac{2}{2}$, 2, 2, 3, 4, 5}. $\frac{2+2}{2}$ = 2.

Soi Non-linear.

 \Rightarrow

Note: -> Conantization is Non-linear operation.

Sumpling is Linear operation.

()

(.)

()

(-

(-=)

(

٦

(:...)

()

0

<u>(</u>.

0

(].

 $\overline{}$

-> Phase - plane Analysis -> Non-linear.

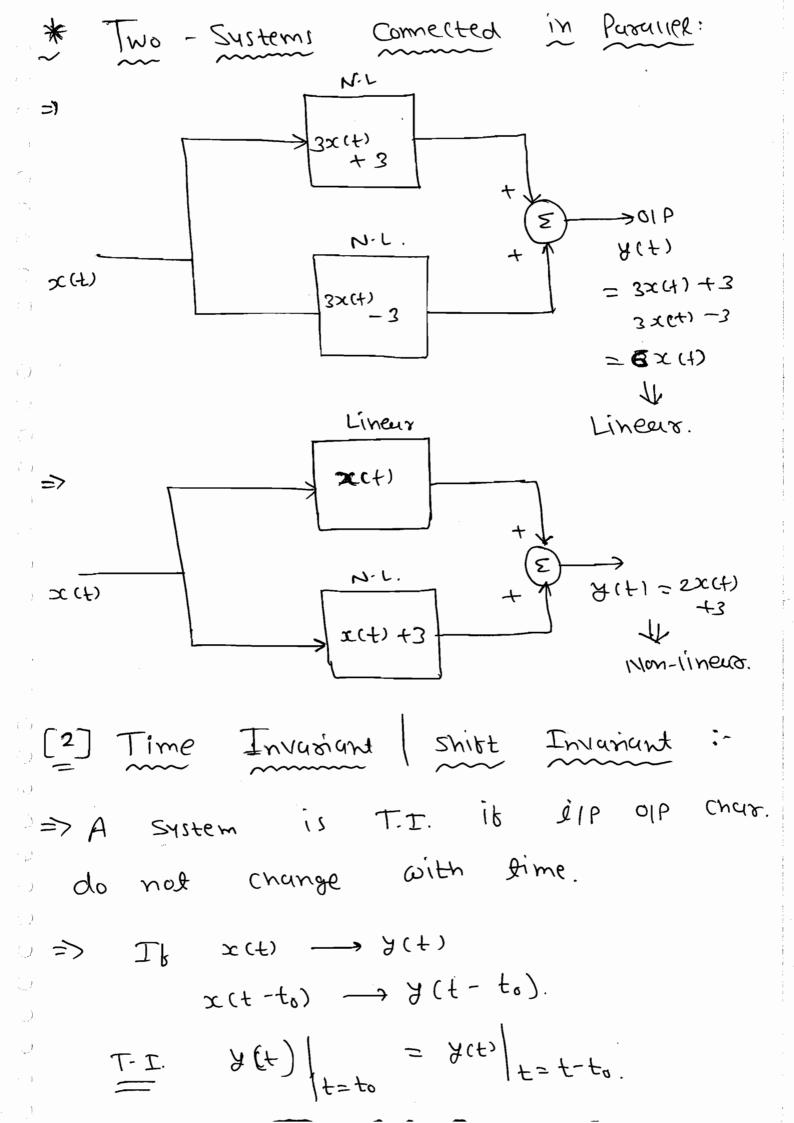
* Two - System Connected in Series.

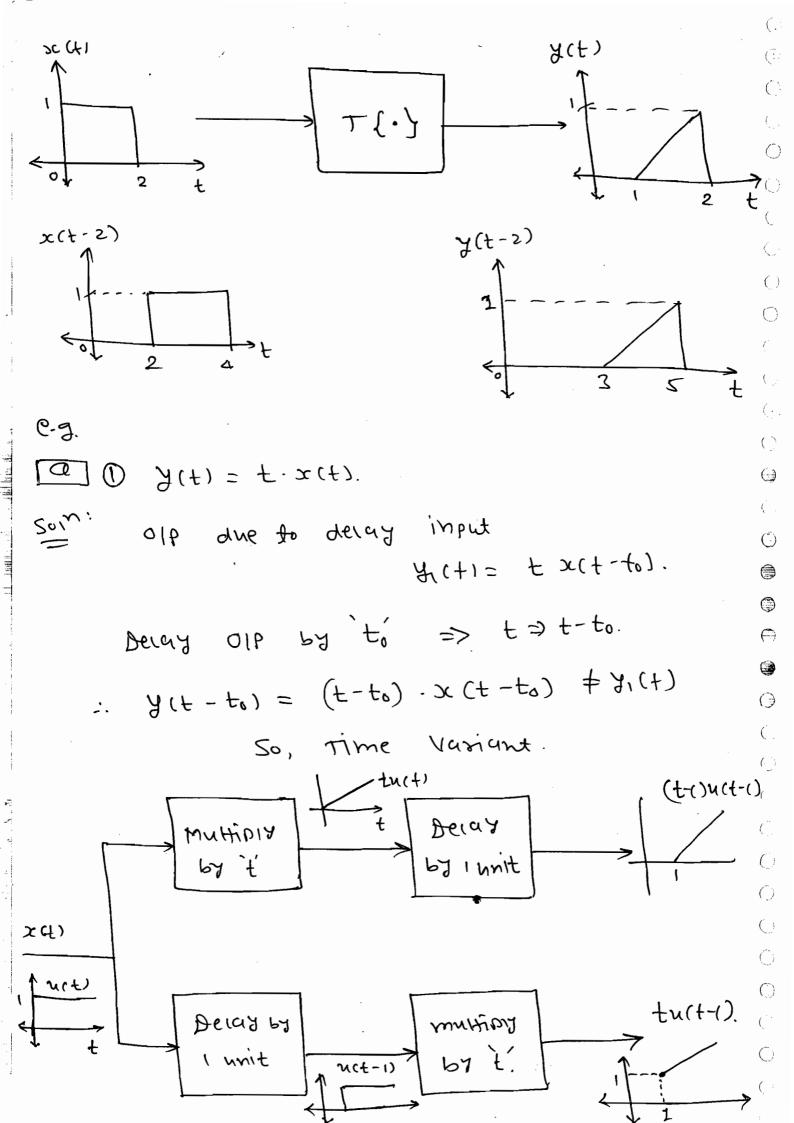
 $\begin{array}{c} S_{1} \\ S_{2} \\ \end{array}$ $\begin{array}{c} S_{2} \\ \end{array}$ $\begin{array}{c} P(t) = x(t). \\ P(t) = x(t). \\ \end{array}$ $\begin{array}{c} P(t) = x(t). \\ \end{array}$

exp. y(t)

Non-lineur.

=> when both S, & Sz are opposite to each other then it becomes linear.





```
A(f) = 6
-x(f)
      Eime Invasiant
               -x(+-+0)
      子(t) =
                -x (+ -to)
     7(t-t0) = e
    \lambda(t) = x^2(t).
      A(f) = x2 (f-f0)
     y(t-to)= x2 (t-to)
        time Invusignt.
     50,
(4) y(t)= x (2t).
Soi Ilp: Y(t) = x (2t -to).
   orp: y(t-t_0) = x(2(t-t_0)) = x(2t-2t_0).
       So, Time Vasiant.
(s) A(f) = x(-f)
        IIP: Y(+) = x(-+-to).
        O(P: Y(t-to) = x (-(t-to)) = x (-t+to).
      So, time Yariant.
> In General,
```

Soin:
$$y(t) = \frac{dx(t)}{dt}$$
.

Soin: $y(t-t_0) = \frac{dx(t-t_0)}{dt(t-t_0)} = \frac{dx(t-t_0)}{dt}$.

(" $\frac{d}{dt}(t_0) = 0$

So. Time Invariant.

(" $\frac{d}{dt}(t_0) = 0$

So. Time Invariant.

(" $\frac{d}{dt}(t_0) = 0$

(" $\frac{d}{dt}($

 \bigcirc

()

(.

 (\cdot)

 \bigcirc

 \leftarrow

3

()

(::

()

 \bigcirc

4 -> 0.V $x_{5}(f)$ + F. A(+) = マンエ.レ Lineur -> First degree of N.L. T-4. dibremantation & -> co-ethicent must be constant or 2 xct). 48(F) = I. V. (here I V- 13 So, Linear time Invariant (L.T.I.) => Because Ub Co-efficient are fixed => T-I. => In any differential ear it ou the Co-epicient are Liked anih mith linear elements that is LTI System. i) IIP OIP depending on time. ->V Time Scaling. -> V iii) Modulator (signal multiply by sine or cos). -> V

 $x_2ct1 = x(t) - x(t-2)$. \Rightarrow LTI CGIVEN). x2(t) = y(t) - y, (+-2). \bigcirc $(\dot{})$ $\chi(t+1)$ ('' => () χ_3 (+) = x(++1) x(4)+ + 5, (+). 50, Y=(+1= 7)(++1) ۴ IJ - XC+). ン(³ (か) 9 \bigcirc 0 2 3 0 1 x, (+1) راخ 2 ¥3(t) (]: 0 1 A(ck) ١ O 2

A x(t) →x(t). => LTI. Initial (ond" y(0)=0. => For a LTI System Sume relation is Varid for ils and OID. [3] Causal and Non-Causal System. => A System is Causal System it the present oil depends only on Present IIP and Past Values of the elp but not on buture values i.e. Causal systems are non-anticipative. eg.: (i) y(t) = (3t+1) x(t). (ii) Acti = xcf). cornof cansal. , a) () Y(t) = sin {x(t)}. Causal. 2 y(t) = x { sin(t)}. sint=0 for t= 1mT, m=0,1,2,... : Y(-11) = >c { sin(-11)} $\xi(-\pi) = x(0).$

 $(\frac{1}{2})$

$$\Rightarrow$$
 $y(-\pi)=x(0).$

olb in exbectived

butuse vaine.

So, MON- Cansal

()

 (\cdot)

(---)

()

 Θ

(3)

(::::

(

C

(,,

(

(

$$S_{11}^{\infty}: \qquad \forall (1) = \int_{0}^{2} x(\tau) d\tau.$$

So, Mon- Cansal.

$$\leq \sum_{i=1}^{n} y(i) = \int_{-\infty}^{\infty} x(i) \cdot di$$
 \Rightarrow Causal.

(a)
$$\forall (n) = \sum_{k=N_0}^{N} x[k]$$
 (b) $\forall (n) \in \mathbb{Z}$

$$Soi^{N}$$
: (ase-I: $N_0 > N$. \Rightarrow Non (ausal (NC).

$$A[U] = \sum_{k=5}^{K=5} x(k) = x(i) + x(i)$$

Case-
$$\underline{\mathbb{H}}$$
: $n_0 \leq N$.

 $y(a) = \sum_{k=1}^{2} x_{k} = x_{1} + \sum_{k=1}^{2} x_{2} = x_{2}$
 $y(a) = \sum_{k=1}^{2} x_{k} = x_{1} + \sum_{k=1}^{2} x_{2} = x_{2}$
 $y(a) = \sum_{k=0}^{2} x_{1} = x_{1} + \sum_{k=0}^{2} x_{2} = x_{2}$
 $y(a) = \sum_{k=0}^{2} x_{1} = x_{2} = x_{2$

: \(\frac{1}{2}\) = \frac{1}{2}\[\times \(\pi\) = \(\pi\)\].

So, Non-causa System.

Mote: Non- Cansa Systems Can not be C design when the independent vuriable is fime. (toon).

0

[9] Y'C++4) + 2(t) = x(++2).

Put +4= 7.

: y'(T) + 2 (T-4) = x (Y-2).

So, Cansal System.

=> Here, Present lime is t+4.

Static Memory less & [4] Dynamic With memory:

=> Static system is that in which of at perficular instand is depend only on input at on that instant only.

-(+13) (1) y(+)= e x(+). Static.

(a) (d) Y(t) = 2x(t) + 3 Steeti (

2) y [n] = g [n+3]. x [n]

Static.

3) Y[m] = x [3M].

Soin: A [1] = x [3] => Dinamic.

Soin: dibterential terms is because of system is energy storing elements

Soi, System is alway dynamic.

=> All Static systems are causa System.

 $(0) \longrightarrow (0)$

Son: Betore applying an input, Old Should not Studt => Comsa.

=> IIP is starring at 0' and oIP is
also starring at 0'. so, cansal system.

 $y(t) = 2 \int_{-\infty}^{t} x(\tau) d\tau$

Causal & Dynamic.

[a] Consider the GIB System shown in time, assume that y [N]=0 for N<0.

 $(\dot{})$

 \bigcirc

0

 $(\dot{})$

 $(\underline{\dot{}})$

(-)

0

0

۰

0

 \bigcirc

 \bigcirc

(..

()

(=):

(.)

(]

=> Find yen) when the Input is (j) x(m) = &[m]. (ii) xcm = ucm].

$$\frac{Soin!}{Soin!} = \infty [n] - \lambda [n].$$

$$\rightarrow$$
 $y[i] = 1 - 0 = 1.$

② x[n] = u[n].

OIP Y ENJ = { 0,1,0,1,0, ... y.

Vlote:

=> Present of depends and an present lip and past input then it is

Finite Impuise Response [FIR].

=> It it also depends on past old it is IIR (Invinite impusse Response)

tilter. FB is there => Recursive.

[5] Stuble & Unstuble Systems:

=> It is a magnitude (oncept.

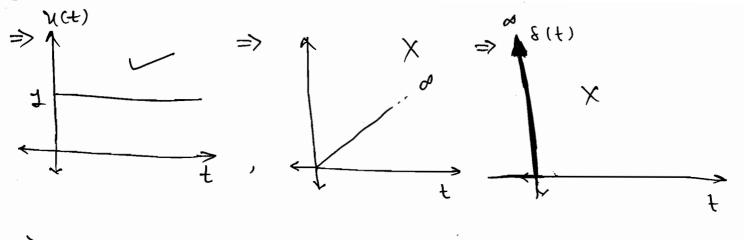
=> Boundedness => Bounded amplitude.

=> B. I.B.O.

 $\mathbb{R} \cdot \mathbb{T} \longrightarrow \mathcal{T} \cdot \mathcal{I} \longrightarrow \mathcal{A} (+).$

If $|x(t)| \leq M_x < \infty$ then \int_{Λ} Stable. |y(t) | < my < 0.

=> For kinite input, of should be kinite



$$tb \propto ct) = N(t)$$

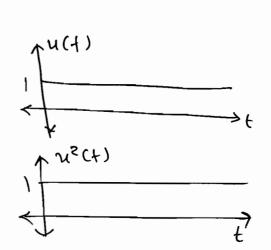
Stuble

$$\rightarrow$$
 $y(t) = (x4)1^2$

 ≤ 0 ,

$$S_{01}^{(n)}$$
 if $x(t) = u(t)$





Unstuble.

(=)

> \bigcirc

 \bigcirc

 \bigcirc

٦

(=)

0

 \bigcirc

@ @ y (t) = d .x(t). Soly: 161, x(+)= n(+). y(t)= d. n(t)= &(t). (Unbounded). So, Unstable. (5) y(t) = x(t). (a)wct. \overline{Soin} : $|\lambda(f)| = |xcf|$ (o) n^{cf} = (xct) |- coscit -> mux vaine t) æ - (. = finite = Stable. (B) y(t)= f |x cys. coswet| at. Soin: A(f) = f (finite) -dt. > Unstable. (7) y(n) = 2x(n) + 3.Soin: Stable linite + finite = finite. => for discrete we have son, 4 mm. [n]x 8 7 [N] = 6 | Soin: | X [n] | = | = | finite => Stuble.

(...

(

(1)

0

 $(\underline{\cdot})$

 \bigcirc

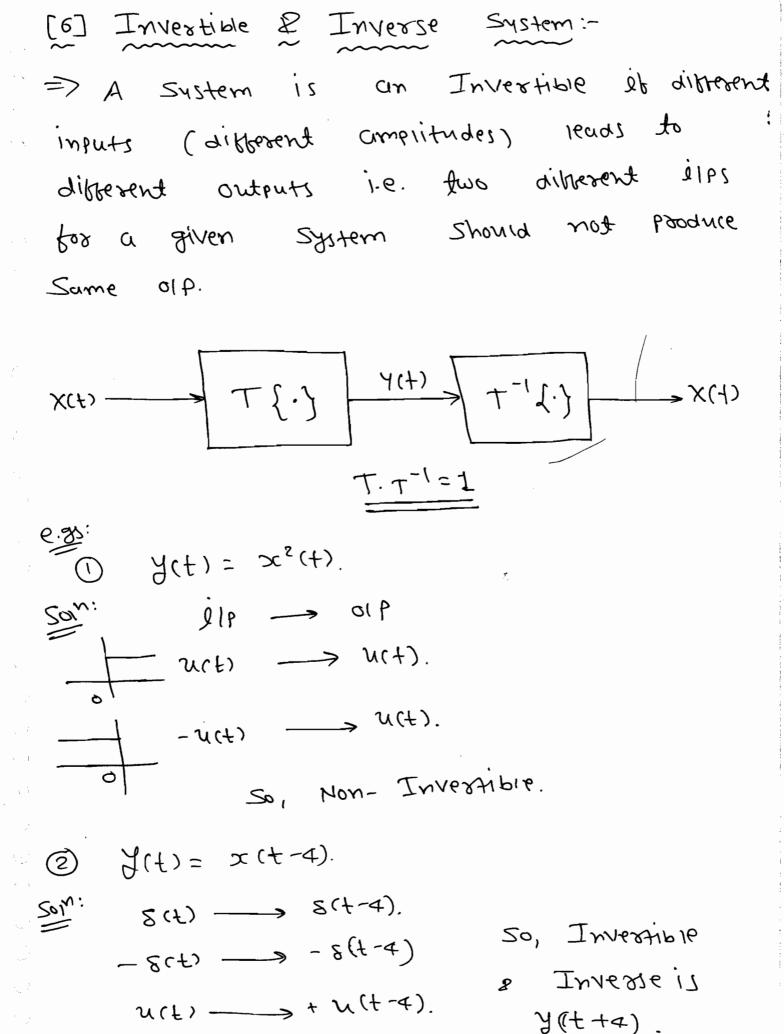
 \bigcirc

()

0

(a)
$$A[n] = \sum_{k=1}^{\infty} x[k]$$
.

$$Son^{*}$$
: $x[k]=1$, $n+n_0$
 $y[n]=\sum_{k=n-n_0} x(1)$.
 pid , $k-n+n_0=m$.



- ~(+) - → - ~(+-4).

3 (x(7)dY. 7(f)= So, Investible élP -> 01 P. Inxerse is $\boldsymbol{\mathcal{Z}}$ 8(7) ay(t) ----> - u(t). - 2(f) ----> f&(f). $\mathcal{U}(f)$ (\cdot) ----- - tu(t). -u(+) * $A(f) = \frac{q}{d} (x(f)).$ JIP. ----> O(P 2 (-) So, Non-Investible. (:-) ()(A) y[n] = n. x[n]. (<u>;</u> lip ----> 01P. ()---> n. s[n] [m] & (~no=0). = 0. S[n] = 0 bearesth of 8(NJ). - 2[m] = 0. E(m) = 0. So, Non- Investible. (3) y[n] = x[n]. x[n-3]. ip --- olp (: S(n) ----> S(n) -0

- 8 Em) - (-8 [m-3]) =0

So, Non- Investebile. A[h]= = x[k]. K=-0 Cont. Discoete $\mathcal{E} \Rightarrow \mathcal{E}$ lip - oip Sin - uin, - STN) -- u(n). So, Invertible. => ilp u[n] $\frac{\gamma}{\sqrt{1+\frac{1}{2}}} \longrightarrow \frac{\gamma}{\sqrt{1+\frac{1}{2}}} = \frac{\gamma}{\sqrt{$ So, Invertible. Inverse is yen - yen-17. $= \sum_{k=-\infty}^{\infty} x[k] - \sum_{k=-\infty}^{\infty-1} x[k]$ $= \sum_{k=-\infty}^{\infty} x[k] - \sum_{k=-\infty}^{\infty} x[k]$ $= \sum_{k=-\infty}^{\infty} x[k] - \sum_{k=-\infty}^{\infty} x[k]$ こ スピル]. (1) A[m] = x[m]. Sin [sum] 11P ---> 01P 8(n) - Sm. sin [57m]. = ZIN (ZUO). E[N) (: N° =0)

= o.

So, Non- Investible. A LTI Systems: Systems is sepresented with respect to impulse response. C'it input is impulse, output is impulse sesponses. => Sibting preperty states that any Signal an be produced as Empiration of smpulses. 6.9. x(s)x(1-4] 8 [1-1] × [1-1] × [1-1] × [1-1] × [1-1] × 8 [n-2) ⇒ Convolution is forma mathematical Operation, just as multiplication, addition and integration. Addition takes two numbers and produces a third number,

while convolution takes two signals and produces a finisa signal. * Continuous Convolution Discrete Convolution. $J(t) = \int_{-\infty}^{+\infty} x(\tau) \cdot h(t-\tau) d\tau \quad J(\eta) = \sum_{k=-\infty}^{\infty} x(k) \cdot h(\eta-k).$ $= \int_{\infty}^{\infty} x(t-\tau) \cdot h(\tau) d\tau, \quad y(\eta) = \int_{\kappa=-\infty}^{+\infty} x[\eta-k] \cdot h(k).$ 24667. Steps: J. X [N] -> X[K], 1. X(t) -> X(T), 2. Forging (XI-K) 2. Folding X(7) 3. Shifting / X[n-k]. 3. Snibting / X (t-r) 4. multiplication /x(t-r).h(r) 4. Multiplation /x(k).h(r). 4. multiplication /x(t-r).h(r) 5. Symmation. S. Integration,

-> By using Convolution we use finding a given state gesponse for the zero System (Zeso initial andition). and and forded -> Siding one signa over the other Ane and snitted version Oß Convolution. concept of signed is a bic2) = 25+57+1 P2(S) = 52+35+4. 2, + 52+1 (Rixeq) 4 +35+ 52 (folding) 28+ \bigcirc 4+35 $313++51_3=21_3$ ()4 + 35+12 --- = 45 + 652+32= 1152 Ę., \bigcirc 4 +31 -= 81 +32 =117 S4+ 553+ 1152+115+4. x(t) * h(t) *Shibting

()

()

(.)

(

 (\cdot)

(:

(·

()

 (\cdot)

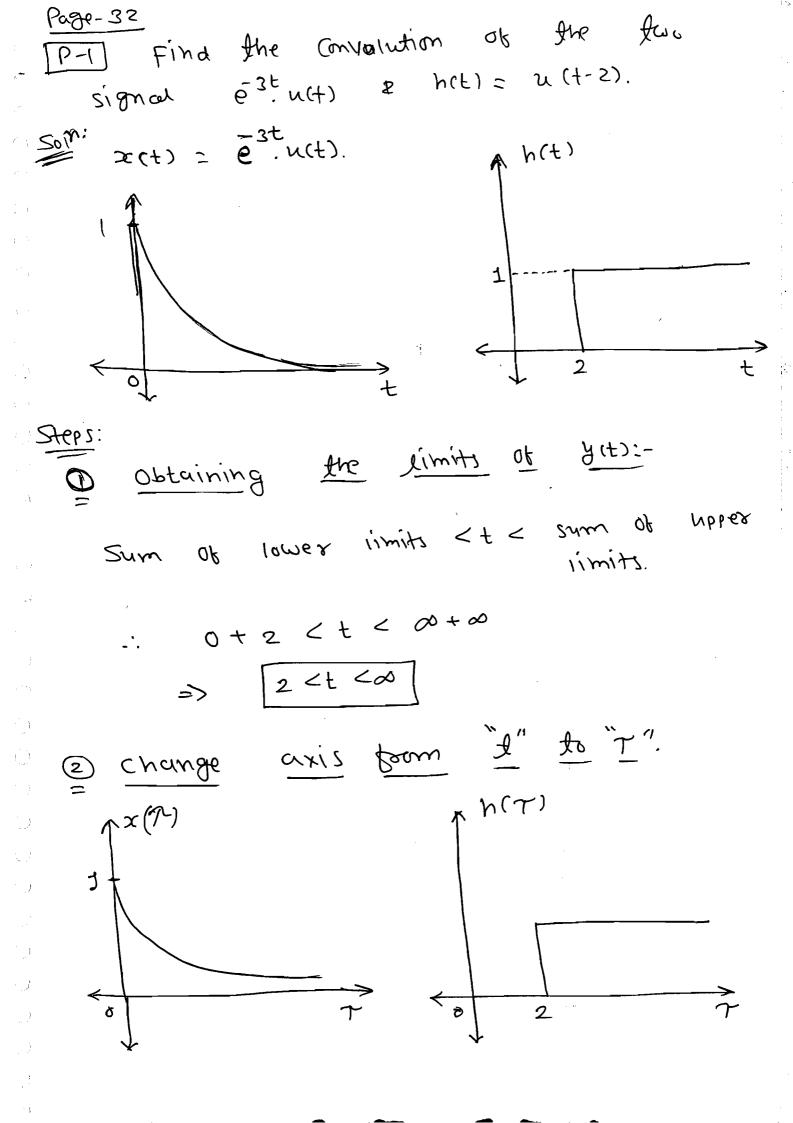
()

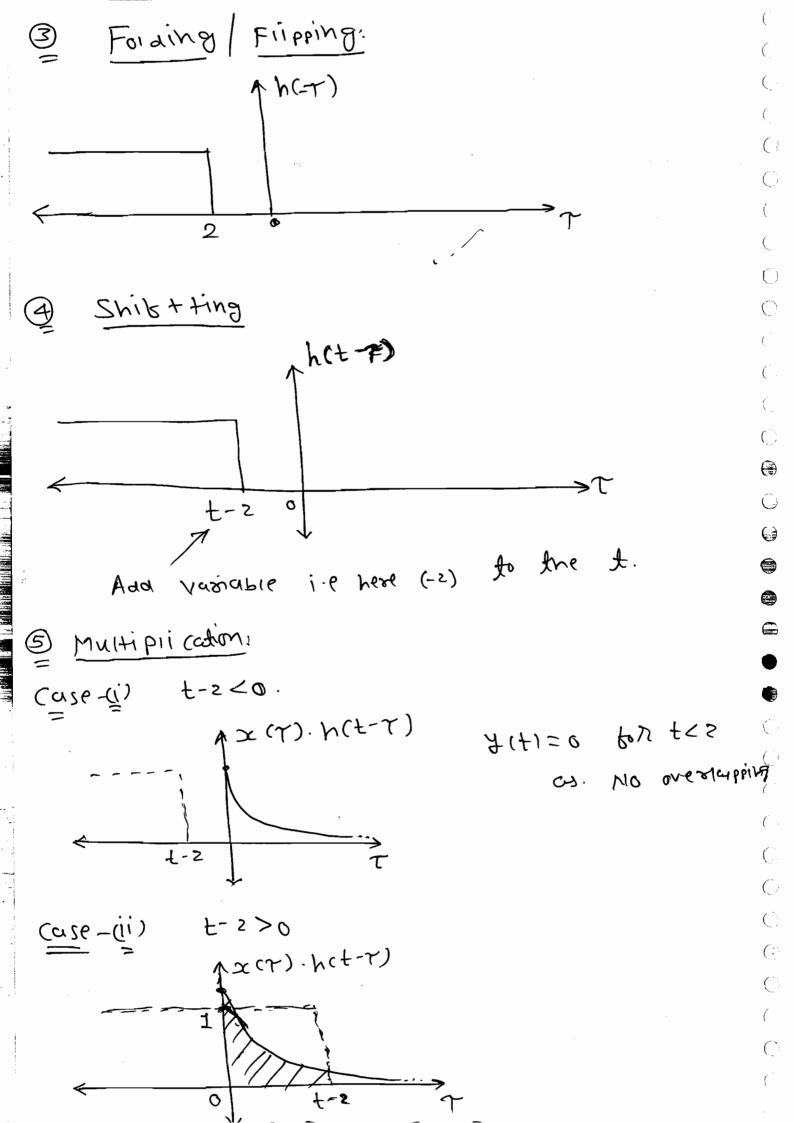
()

()

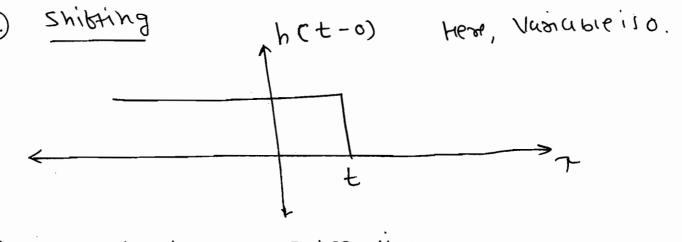
 (\cdot)

x (7), h (t-Y) d7 O tolding -OMULTIPII Cation. 4 Integration.

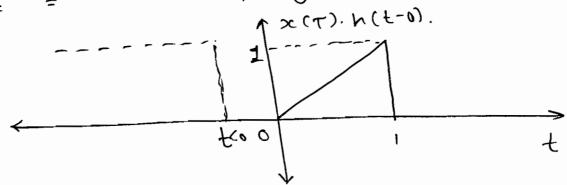




 $e^{-3\gamma}$ uct). $d\gamma$. => \ \ \ \ \ \ (+) = $\frac{3}{1-6}$ (+) g Cansal System -> Convolution of two is (ansal. [a-2] Find the Convolution of the signals Zhown in figures (h(t)=1, t>0. $x(t) \uparrow = t$, 0 < t < 10 +0 < t < 1+00. => (0< t<0) h(T)=1, $\int x(\tau) = \tau , 0 < \tau < 1.$ h(~~)



$$(\sigma^{26}-(\bar{i}) \qquad f < 0 \implies A(f)=0$$

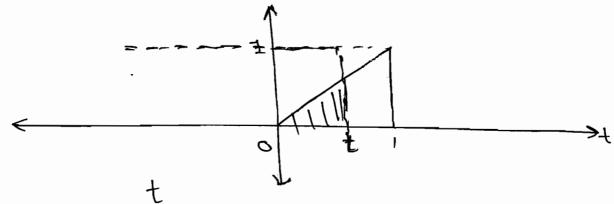


(

0

 \bigcirc

()



$$\lambda(f) = f_{5}|_{5}$$
; $0 < f < 1$.

$$y(t) = \int (\tau) \cdot (\sigma) d\tau = \left[\frac{\tau^2}{2}\right]_0^1 = \frac{1}{2}$$

So,
$$y(t) = 0$$
, $t < 0$

$$= t^{0}|_{2}, 0 < t < 1$$

$$= |_{2}, t > 1.$$

[P.3]

An(t)

$$\frac{1}{3}$$

$$x (t) \cdot h(4-t)$$

$$\frac{1}{2}$$

$$\frac{1}{2}$$

$$\frac{1}{3}$$

$$y(t) = \int_{S} (t)(t) \cdot dt = 1.$$

(-)

٠

(:)

()

$$y(t) = \int x(\tau) \cdot t(0.5 - \tau) \cdot d\tau$$

```
Page-33
[P2.1.4.] Suppose Zeti= (x(-7+a) h(t+r) dr.
               S(t) in Jesus of A(f) = X(f) * N(f).
  Ex 68627
 , 501~:
                   七ナヤニ 入.
            take
                    => t= λ-T. dt=dλ
                        -r = t-x.
          A(f) = X(f) * K(t)
                 = \int_{-\infty}^{\infty} \chi(t-\tau). \, \mu((\tau). \, d\tau.
                 = \int_{0}^{\infty} \chi(\tau). \ k(t-\tau).d\tau.
         Z(t) = \int_{-\infty}^{+\infty} \chi(t-\lambda+a) \cdot h(\lambda) d\lambda.
               = ) x ((t+a) -0), h(0) d().
       : Z (+1 = x(++a) * h(++a).
  P2.1.5.
         x(f+2) * 8(f-7)= -
    (4)
          X(f) * 8(co +p) =
   (d)
             ×(++5) * 8(+-7)
          <u>a</u>
              = \chi(f+2-4) \quad ( :: \chi(4) * 8(f-f9)
                                        = x(t-t).
               = x(t-2).
```

.

(.

0

()

()

()

۱

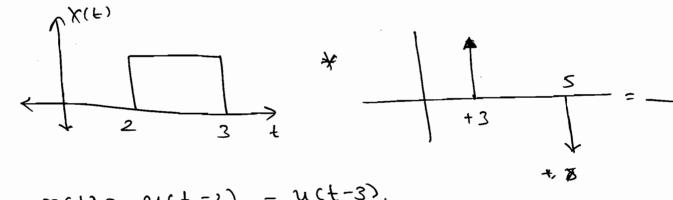
 \bigcirc

(:

(Î)

()

()



$$So_{\nu}$$
: $x(t) = x(t-s) - x(t-s)$.

[0]

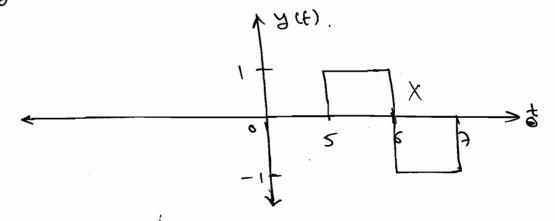
i ')

..)

$$= \lambda(t-2) - \lambda(t-6) + \lambda(t-3) - \lambda(t-6),$$

$$= \chi(t-s) - \alpha(t-s) + \chi(t-s) + \chi(t-s)$$

$$= \chi(t-s) - \alpha(t-s) + \chi(t-s)$$



$$X(f) * 8(f-f^{0}) = X(f-f^{0})$$

$$= x(f-13)$$
.
= $x(f-13)$.

$$= \frac{1}{2} \cdot \left[x(t) * 8 (t + 312) \right]$$

$$= \frac{1}{2} \cdot \left[x(t) * 8 (t + 312) \right]$$

$$= \frac{1}{2} \cdot \left[x(t) * 8 (t + 312) \right]$$

$$= \frac{1}{2} \cdot \left[x(t) * 8 (t + 312) \right]$$

$$= \frac{1}{2} \cdot \left[x(t) * 8 (t + 312) \right]$$

$$= \frac{1}{2} \times \times (\pm \pm 3/2).$$

P 2.1.3. (b)

The impulse Bespanse of the Continuous time System is given by h(t) = S(t-1) + S(t-2).

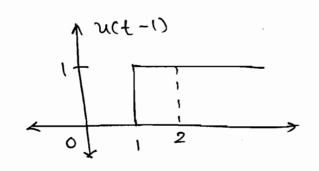
The value of the Step Bespanse at t=2 is.

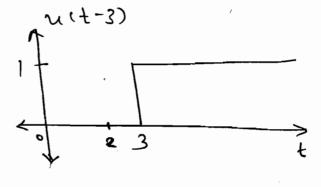
a) 0 (B) 1 (c) 2 (D) 3.

Soin:
$$x(t) = h(t)$$
.

$$\exists (t) = \chi(t-1) + \chi(t-3).$$

$$\exists (t) = \chi(t-1) + \chi(t-3).$$





 \ominus

()

()

```
[P2.1.6] Explain the difference between the
following operation ! ?
        [ etuce)] sct-1).
    => it is product property of impulse
       i.e. X(t). S(t-to)
= X(t-to). 8(t-to).
     so, | et. u(t)] 8(t-1]
        = e^{-1} u(1) \cdot S[t-1] \quad (:: t_0=1].
         = e'. 8[t-1].
  (b) + 0 e-t. n(t). 8(t-1) at.
  => It is a sitting property of impulse.
    i.e. | = x(t.) at = x(t.)
                                    ; t, < t 0 5 t2.
    50, +00 =t. u(t). S(t-1) at
          \frac{-\infty}{e^{-1}} u(1) ( : t_0 = 1 + x(t) = e^{-t}u(t)
                             ₽ - 0 < 1 <+0).
  (c) e n(t) * 8(t-1).
```

=> It is the Pro Convolution property Ob Impulse. i.e. $|\chi(t) * 8(t-t_0) = \chi(t-t_0).|$ So, Etu(+) * 8(+-1). = (t-1)= e . w(t-1). | P2.1.7 Let X(t) = N(t-3) - N(t-5) & $h(t) = e^{-3t} \cdot h(t)$. Find $\frac{d}{dt} x(t) * h(t)$. $\chi(t) = \chi(t-3) - \chi(t-5).$ $\frac{\partial f}{\partial x(f)} = 8(f-3) - 8(f-2).$ \$ xxxx * xxxx) = \(\(\(\) \ (K-8) -X(K-8) - M(+-2) * 8(+-3) + M(+-2) * 8(+-2). = u(+-6) u(+-10) - u(+-8) -+ u(+-10). MOW, dx(t) * h(t). $= [8(f-3) - 8(f-2] * e_{3f} n(f).$ $= e \cdot n(t) * 8(t-3) - e^{3t} n(t) * 8(t-5)$ $= e^{3(t-3)} \cdot u(t-3) - e \cdot u(t-5)$

 \bigcirc

(;

Mote: In LTI Sustem, whatever happens in i.e. $\frac{d}{dt} \chi(t) * h(t) = \frac{d}{dt} \chi(t)$. $= \Rightarrow \text{ In general,}$ $= \chi^{m}(t) * h^{n}(t) = \chi^{m+n}(t)$ $= \chi^{m}(t) * h^{n}(t) = \chi^{m+n}(t)$

i.e. Whatever be the delay in input Same delay will occur in olp of it

is time Invusiont system.

Brook; A1f) = (>(L), A(f-L) qL.

Asea An = $\int y(t) dt = \iint x(\tau) h(t-\tau) d\tau$.

= $\int x(T) dT \cdot \int h(t-T) dt$.

: | An = Ax. An. | => Scaling: $X(\alpha t) * h(\alpha t) = \frac{1}{|\alpha|} \cdot A(\alpha t)$ Mote:
In above (ase, property is varid only when the scaling fuctor in & N Should be sume. X i.e. if x(Qf) * h(Bf) = 8. d \$ B then No Comment. $u(t) * u(t) = f \cdot u(t)$ u[n] * u[n] = (n+1)u(n]. $\mathcal{E}(f)$

$$\frac{S(t)}{u(t)} > \frac{t}{\int_{-\infty}^{\infty} (1) d\tau} \frac{u(t)}{v(t)}$$

 $(\exists$

(----

0

(

$$\frac{8[n]}{u(n)} = \frac{n}{k=-\infty}$$

$$\frac{n}{k=-\infty}$$

$$\frac{n}{k=-\infty}$$

$$\frac{n}{k=0}$$

$$\frac{n}{k=0}$$

$$\frac{n}{k=0}$$

$$\frac{n}{k=0}$$

$$\frac{n}{k=0}$$

$$\frac{n}{k=0}$$

$$\frac{n}{k=0}$$

$$\frac{n}{k=0}$$

$$\frac{n}{k=0}$$

Convolution ob U[n] with u[n-4] ct n=5. 11 - 8 Y[n]= U[n] * U[n-4]. $= \binom{m+1}{-4} u [m]. = (\underline{m+1-4}) u [m].$: 4[5]= (5+1-4]. : y(5) = 2. [u(t+1) - u(t-3)] * [n(t+1) - u(t-1)].= SON, A(F) = N(F+1) * N(F+1) - N(F+1) * N(F-1) - U(t-3) * U(t+1) + U(t-3) * U(t-1). = & (f +1+1) - & (f +1-1) - & (f-3+1) + 8(+-3-1). 8(2+2) -8(1) -8(t-2) +8(t-4). ACF). 1 = 2x2 = (1) Az = 12 x2 x2 = 2 $\mathcal{F}(f)$ h(f). so, Ay= Ax. An

Note: -> Convolution of two unequal length de (tangular functions es a Trapezium.

-> It length is sume then it is a toungre.

()

(..)

 \leftarrow

-> Convolution of the tunction ito it selb is equal to integration Ob that to. This statement is Varid only for unit step to $\kappa(f)$. i.e. $\chi(t) \times \chi(t) = \int \chi(\tau) d\tau$.

u(t) * u(t) = v(t)= t·u(t)= [u(r)dr.]

where, x(T)= x(T).

* Convolution using Differentiation: y(t) = x(t) * h(t).

 $\frac{dA(f)}{dA(f)} = \frac{dr}{dx(f)} * h(f)$ (OK)

$$\Rightarrow \begin{cases} \frac{dy(t)}{dt} = x(t) * \frac{d}{dt} h(t). \\ \frac{d}{dt} = \int_{-\infty}^{\infty} \left[x(t) \cdot \frac{d}{dt} h(t). \right] dt. \end{cases}$$

$$\begin{array}{c} (2) \\ (2) \\ (3) \\ (4) \\ (4) \\ (4) \\ (4) \\ (4) \\ (4) \\ (5) \\ (4) \\$$

$$V(t) = V(t-5) - V(t-1)$$
.

$$\Rightarrow \frac{d}{dt} \cdot h(t) = \frac{8(t-2)}{-8(t-3)}$$

$$= X(f) * \frac{\partial f}{\partial r} [n(f-s) - n(f-s)].$$

$$\Rightarrow \frac{\partial f}{\partial r} = X(f) * \frac{\partial f}{\partial r} [n(f-s) - n(f-s)].$$

$$= \chi(f) * g(f-s) - \chi(f) * g(f-3).$$

$$\frac{\text{qA(f)}}{\text{qA(f)}} = \chi(f-s) - \chi(f-3)$$

$$\Rightarrow y(t) = \int_{-\infty}^{\infty} [x(t-2) - x(t-3)] dt.$$

$$\Rightarrow y(t) = \int_{-\infty}^{\infty} [x(t-2) - x(t-3)] dt.$$

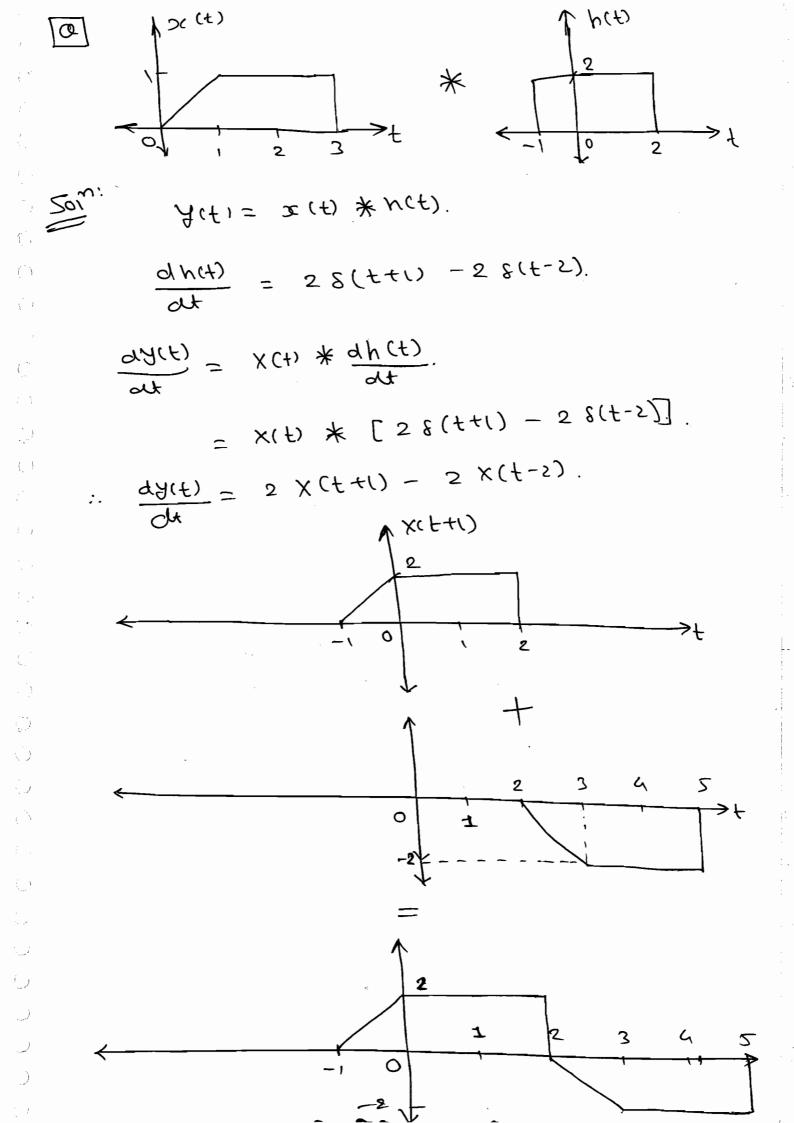
$$\Rightarrow y(t) = \int_{-\infty}^{\infty} [x(t-2) - x(t-3)] dt.$$

$$\Rightarrow y(t) = \int_{2}^{\infty} 2 dt = 2(t-2).$$

$$\Rightarrow y(t) = \int_{2}^{\infty} 2 dt = \int_{2}^{\infty} 2 dt + \int_{2}^{\infty} 2 dt.$$

€

()



So,
$$y(t) = \int_{-\infty}^{t} \frac{dy(t)}{dt} dt$$
.

NOW, $(ase - (i)) : -1 \le t < 0$.

 $y(t) = \int_{-\infty}^{t} 2(t+i) dt$
 $= [t^2 + t]_{-1}^{t} = t^2 + t - 1 + 1$
 $= t^2 + t ; -q \le t < 0$.

 $(ase - (ii)) : 0 \le t < 2$.

 $y(t) = \int_{0}^{t} (2) dt = 2t ; 0 \le t < 2$.

 $y(t) = \int_{0}^{t} (-2(t-2)) dt + 4$.

 $y(t) = \int_{0}^{t} (-2t+4) dt + 4$.

()

(

(Case-(iv): 3 ≤ t < 5.

$$y(t) = \int_{3}^{4} (-2) dt = -2 (t-3) = 6-t.$$

$$y(t) = t^{2} + t ; -1 \le t < 0.$$

$$= 2t ; 0 \le t < 3.$$

$$= 4t - t^{2} ; 2 \le t < 3.$$

$$y(t) = 6 - t ; 3 \le t < 5.$$

Assume $g(t) = x(t) * h(t).$

$$tet, x(t) = u(t).$$

$$h(t) = s(t).$$

$$g(t) = h(t) * s(t).$$

$$\partial_{\bullet}(f) = \rho(f)$$
 (: $f^{\circ} = 0$).

$$g(t) = \int_{0}^{t} t \cdot dt = \frac{t^{2}}{2} \cdot u(t).$$

(:[PZ:1.8] An Input signal x(t) Shown in tigure is applied to the System with ≥ 2(f-3N) Find impuse sesponse hcti= ()(... n=-0 the output. X(+)2 (f-3N). +8(F) + 8 (++8) + 8(++3) +8(f-3) 0 +8(f-e) +-.. C_{J} 0 +8(f) $\chi(t) * h(t).$ J(t1= x(t) * (... + E(f+e) + E(f+3) + E(f-3)+ 8(+-6) +--). : $A(f) = \cdots + x(f+e) + x(f+3) + x(f-3)$ (___ + x(f-e) +... 7(4) =) 0 0 3 ()(]

Mote: Convolution of a general signed aidn periodic train of impulses is pesiodic sepectation of general signal. >> System length should be the more than the input signal length so that se can retain the information without distroting. * Discrete Convolution: P2.111 Consider the signed h(n) = [1]. [[[[-1]]] - V[N-10]] Such that $h(n-k) = \left(\frac{1}{2}\right)^{n-k-1}$, $A \le k \le B$ o ; eigewhere Find A

BBP $h(n) = \left[\frac{1}{2}\right]^{n-1} \cdot (n) : -3 \leq n \leq 9.$: $h(u-k) = \begin{bmatrix} 5 \\ 1 \end{bmatrix}$; $m-3 \leq u-k \leq 3$ -3-n < - k < 9-n. [P 2.1.12] A linear System with Imput output y(n) related as X(N) & X(K), g(n-2k) Where y (n)=

g(m) = N(N) - N(N-4) . Find y(n) $[r_{1}]_{X}$ X(N) = 8 (N-5) (S-N)38 = [N)X128P, => x (27 = 1 : y(m) = x(z). g (n-4). 8[m = 8 (n-4) y[n) = & u[n-4] - u[n-8]. y cms 1 time vasiant. system is -> above Discrete Impusse. Property Ob Convolution X(n) * 8(n-no) = X(n-no).

(3)

()

(

O

(:

(÷.

|P2.1.14 | Find the convolution of x(n)= d 1,2,3,4) & h(n) = d1,2,1,-1).

205 pierre methods Soin: There are total four Convolution:

- 1) Silding Stoip. 3 sum by Comm.
- Portanial division 2) Array method A Recursive Division.

Column: Rd **=>** 3 1 = [m]x 2 1 -1 h[n] = 1 23 2 4 6 8 3 2 -2 -3 -4 -\ J(N)={1, 8, 13, 9, 1, -4}.

(

0

Polynomial Division method:

1 (1) 2 (3) 4)

@ Recursive Bivision:

=)

J[n] = \(\times \times (n-k) \cdot h(k).

~=0 A[0] = X(0). N(0).

= A[1] = x[0] · P[1] + x[1] · P[0]

7=5 A C5J = XE0J. PC0J + XE1J. PC1J

* Deconvolution (System Identification): JIB >C[N] = {1, 2, 3, 4) 0 O) P (N) = { 1, 4, 8, 11, 3, 1, -4}. h [m] = 9. Method-1: Sum by Column: $\rightarrow \times [n] \rightarrow 1$ 3 4 2 h [m] d Ь 9 \mathcal{C} 20 30 49 a 26 36 46 b 26 36 _ 40 bB 39 d X (~) 1 11 9 4 8 => \a=1, \a=-1 2445-4 2+6=4 34+26+(= 8 38+4+ (= 8 h (n)= {1,2,1,-1}. : C=I Method- 2: Recursive division: YEM= EXEM-KJ. HEKJ. => n=0 y [0] = x [0] x To]. → bind k(0) A CO] = X CO] · P CI] + X EI] · N CO] → PUNG .

h [1].

A COJ. WCO) + X COJ P CO] + XC2J· h [6].

Method-3: Porynomica divisim.

x[n] = & 1, 2, 3, 4}. y [n] = { 1, 4, 8, 11, 9, 1, -4}.

1+20 + 62 - w3

1+200 +3002 + 4003) 1+400 + 8002 + 11003 + 9004 + 005 + 4008

1 +2w + 3w2 + 4w3

26+ 365 +763 +964 +65 =406

20 +402 + 603 +804

0 + 1 w2 + 1 w3 + 5 w4 + w5 + 4 w6

_ W2 +2 W3 +3 W4 + 4 W5

- 62 + 2 W4 + 6W5 - 4W5

ω3 - 204 - 6ω5 +4ω6

(---

(;)

=

 \bigcirc

(:

0

So, /h [n] = {1,2,1,-1}.

Periodic (02) * ordinary circular convolution. Convolution 2 X2 [N] -> Ms Sambler (5) Nb (N) -> Ms 1 yptn) -> max. (n, m2) $y [N] \longrightarrow (N_1 + N_2 - 1).$ [Find Periodic (or) cidence Convolution of xp[n] = {1 23 43 & pp(m) = 1 1 2 1-1]. xp(N)= 123 hp(n) = 1 2 1 ordinary and = 1 4 8 11, 9 1 -4 Words around last + 9 , -4 0 haif of y my 10 5 4 11 Periodic Conv. oip 7[n]. Note: Lineur conv. + Airusing = periodic conv. => Matrix method: [123412341234] 2 1 4 3 2 = [0 5 4 11]

P2.1.17] Criven X=[a,b,c,d] as the input to un LTI System produces an output y=[x,x,x,x,... repeated n times]. The impulse ()sesponse of the system is ---. A=[apca apcq apcq ··· b 8(m) 8(m-4) 8(m-8) -- times] $8 = \sum_{N=0}^{N-1} S(N-4i).$ Given $A(f) = e^{f} \cdot n(f) * = e^{f} \cdot n$ K=-0 Y(t) = Ae box 0 st < 3 find A? Act) = et.n(+1) * [-.. + 8(++6) + 8(++3) + 8(+) + 8(+-3) +8(+-4) 50, g(t)=+-+e n(t+6) + e ... n(t+3) tet. n(t) + e (t-3) - (t-6) + e · n(t-6) (: $\left(\cdot \right)$ as y(t) = Aet for 0 st <3 y(t)= Aet = ... + e + e + e + e. () $\left(\cdot , \cdot \right)$

$$A = 1 + e^{3} + e^{6} + e^{9} + \cdots$$

$$A = \frac{1}{1 - e^{3}} \qquad (-A_{n} = \frac{a}{1 - A_{n}}).$$

[P2.1.18] Suppose for an L.T.I. System it

the input appried is S(n) - S(n-1),

the output is observed to be S(n) - S(n-1)+2S(n-3). Find the output one to the

input 7S(n) - 7S(n-2)?

K'(M-1) = R(M-1) - R(M-5).

$$X_{1}(N) + X_{1}(N-1) = S(N) - S(N-5).$$

$$50, \times (N) \longrightarrow S(N-1) + 28(N-3).$$

$$= 78(m) - 78(m-1) + 148(m-3) + 7(8(m-1)) - 78(m-2) + 148(m-4).$$

* Properties of LTI Systems: (<u>ansar</u>: => Before the application or input the autoust of smpulse at 20=0. We can not get the output as impulse sesponse pefore n=0. i.e. p(n)=0 for n<0. $\chi(t) \longrightarrow \chi(t)$ => OIP hcm = I. Response = 0 ; ~< 0. ∫ | him) ar < ∞ = limite. \$ | h(m) < 0. $|y(t)| = \int |x(t-r).h(r)| dr$ Proot. = [x(+-r)]. [x(+-r)].dr - 0 finite B. I. B. O. = binite. +00 | h(r) dr

-a livite.

()

()

()

()

(=)

0

0

(]

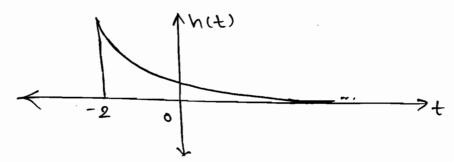
.. Area under absolute value of impulse sesponse is limite.

h(t) = K 8ct).

$$(0t)$$
 $h(t) = 0$, for $t \neq 0$.

Note: An Property indicate interned behaviour of the system.

Soin: het)= et. n(t+2).



n(t) = 0 for t<0. So, Non-Causal.

Som: h (m) = 3 ; n > 2.

=> $\leq 3^{n} = 9 + 27 + 81 + \cdots = 0$. = Unstable. ()-> hons is define for positive index, n (=> (ansal. [P2.2.4.] The sunge ob a and b for the ٥ Impulse sessonse $n(m) = \begin{cases} c^m & 3 & m \ge 0 \end{cases}$ to be stable is Soln: [0-2,2.5] Criven N(t) = eatu(t) + est N(-t). Find dt X & B tor βt h(t) = e · u(t) + e · u(-t). stuble. i.e. (- : ~ (+) / .dt. (:) (-) ()()($\begin{bmatrix} \frac{1}{6} \end{bmatrix}$ + $\begin{bmatrix} \frac{-3}{6} \end{bmatrix}$

$$= \frac{1}{4} + \frac{1}{3}$$

$$= 7/12 \cdot = \text{binite.}$$

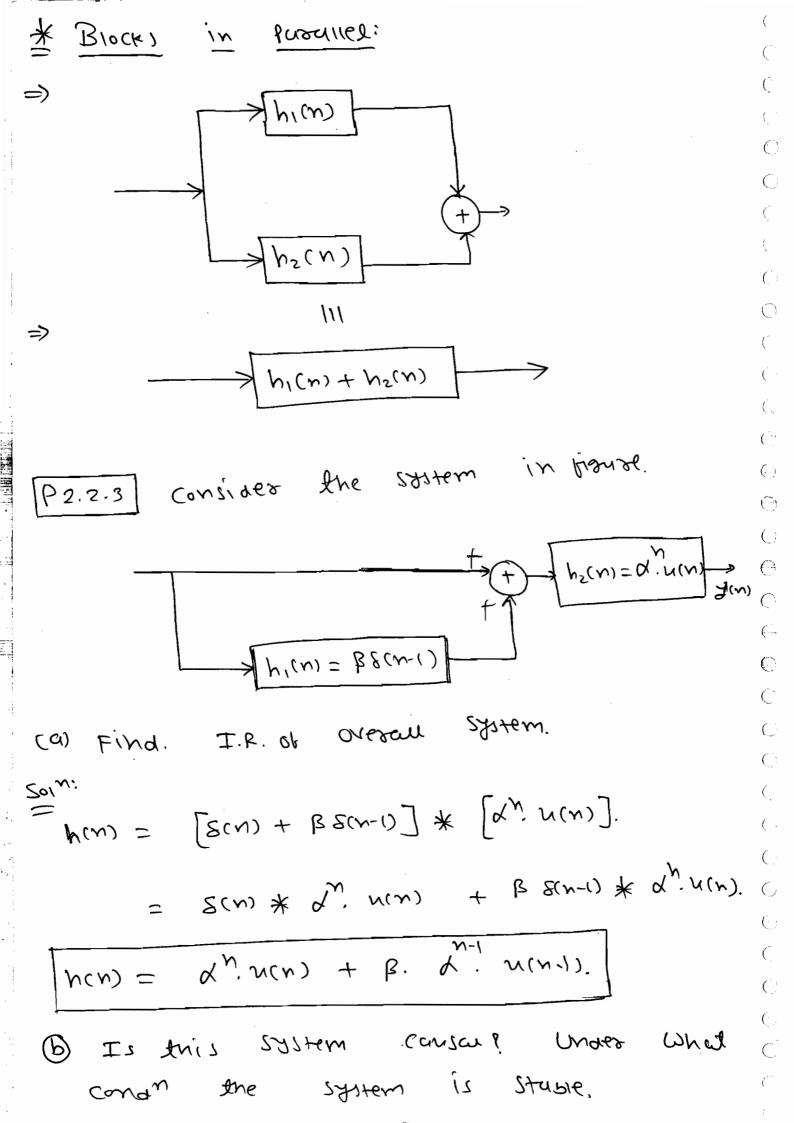
Solve of P 2.2.4. :

$$\text{for Stable:} \qquad \sum_{n=-\infty}^{\infty} n(n) = \text{binite} < \infty.$$

$$= \sum_{n=-\infty}^{\infty} \sum_{n=-\infty}^{\infty} n(n) = \sum_{n=-\infty$$

$$\Rightarrow \sum_{m=1}^{\infty} \frac{b^{m}}{b^{m}} = 1 + \frac{b^{1}}{b^{1}} + \frac{b^{2}}{b^{2}} + \frac{b^{3}}{b^{3}} + \cdots$$

$$\frac{1}{h'(u)} + h'(u) = \frac{1}{h'(u)} + h'(u)$$



=> yes, system is causal. => Ib Id/<1 then system is stuble. Shown [P2.2.6] For the interionneited Statem it lig. find the overall imprise response. $\frac{\partial}{\partial x(x)} = \frac{\partial}{\partial x(x)} = \frac{\partial}$ Soin: for impuise response x(n)= 8(n). :. hcn) = [8cn) - \frac{1}{2} 8cn-1)] * [(/2) ncn)]. = S(n) * (=) ", n(n) - = S(n-1)*(=)", h(n). $= \left(\frac{1}{2}\right)^{n} \cdot u(n) - \frac{1}{2} \cdot \left(\frac{1}{2}\right)^{n-1} u(n-0)$ $= \left(\frac{1}{2}\right)^{n} \cdot \left[N(n) - N(n-1)\right].$ $= \left(\frac{2}{7}\right)_{\mathcal{N}}. \quad \mathcal{Z}(\mathcal{M}).$ $= \left(\frac{2}{7}\right), \quad \xi(\lambda).$ = 8(m).

```
[P2.2.2] Consider the System s, in with
 I.R. hcm = (1/5), w(n).
 (a) Find A' such that kim =
     h(m) - Ah(m-1) = 8(m)
     h(m) - Ah(m-1) = 8(m)
    \therefore \left(\frac{1}{5}\right)^{\gamma} \cdot \kappa(\gamma) - A \cdot \left(\frac{1}{5}\right)^{\gamma-1} h(\gamma-1) = \delta(\gamma).
            A should 1/5 so that
         (+) n[n(n) - u(n-1)] = 8(n).
           : A=1/5
(b) using sesult from past-(a), determine
the I.R. g(m) of an LTI system Si
which is imvesse of SI.
          h(n) * g(n) = g(n)
                   g(m)= h Inv(m).
     there h(n) - Ah(n-1) = \delta(n).
          h(n) * [ 8(n) - A 8(n-1)] = 8(n).
                      hin = 9(n).
     .. g(n) = 8(n) - A8(n-1).
```

(

()

 \bigcirc

(:)

()

()

=> A[n] = ux[n] T.V. Nen. Investible $\Rightarrow \lambda(\omega) = x(\omega) \times (\omega-3)$ ML N.I. $= \sum_{n \in \mathbb{Z}} y(n) = \sum_$ T.V. N.L. 10.T. $y (m) = \sum_{k=-\infty}^{+\infty} x(k)$. $\Rightarrow Inverse is$ L.T.I. System. 7[m] - 7[m-1]. Mote: Impuse sesponse from is varied only for LTI System. X(k) = S(k) = A(k) = h(k)if him= win). $h(n) * h_{inx}(n) = 8 [n].$ $\frac{1}{1} \cdot \frac{1}{1} \cdot \frac{1}$ [P2.2.7.] Determine whether each of the tollowing Statements are TRUE (or) FALSE. 1) The Cosecade Ob 4 non Causa LTI

J

SAREM MILL CHURCH WE IT NECESTANIA

non Causal. \$ 8cn-2) ~ u(n+2-2) = u (m-3). causa these is chance of cansuity. So, Statement is fulse. 2) It am LTI System is causa, it is stable. let, heti= net) -> LTI & causa. ∫ | n(+) | = | (1) at = ∞ But = unstable So, Faise Statement \bigcirc 3) It hat is the I.R. of an LTI statem \bigcirc \in Which is Periodic & non-zero, the Systemo es unstable. An Periodic signal are ever lusting Signa. => Unstable Statement is Tome.

()

()

(

(·`)

 \bigcirc

(

(::)

 \bigcirc

(::

 (\cdot)

()

()

()

()

(··

* Step Response:

-> total internal penarious of statem is

chasa, by I.R.

-> Sudden change in Statem behavering is char. by S.R.

hiti=
$$\frac{d}{dt}$$
 S(t).
S(t) = $\int_{-\infty}^{t} h(\tau) d\tau$.

$$\Delta(t) = \lambda(t-2)$$
 & h(t) = e^{-3t} h(t).

So M:

$$= \left[\frac{e^{-3\gamma}}{e^{-3}} \right]^{4}$$

$$= \frac{3}{1-6}$$

$$= 3(f-5) = 9(f)$$

 $S(H) = \frac{1-e^{-3t}}{3}$

Mote: whenever the one signal is step signal then we an find our by just integrating other signal.

System if the Step response is S(t) = (0) wot u(t).

= I.R. $h(t) = \frac{d}{dt} (S(t)).$

: h(t) = d[coswot. n(t)].

.. het)= -wo sincot. u(t) + coshot. 8(t).

= - Wo sin wot. u(4) + [cos(wo-0)] . 8(4)

 \bigcirc

 \bigcirc

()

(:

: h(t) = - 6, sin o ot. u(t) + 8(t).

[P2.3.4] It the unit step response of u System is (1-e^{-dt}) ucts, then its unit

soin: $s(t) = [1 - e^{-\alpha t}] n(t)$.

.: h(t) = d. S(t).

= d[n(+) - e. n(+)].

= 8(t) - e. s(t) + xe. uct).

$$= 800 - e^{-0}8(t) + 0.e^{-0}u(t).$$

$$= x \cdot e^{-0}u(t).$$

P2.3.1.) Find the Step response of the System is the impulse response is $h(n) = (0.5)^n u(n)$.

Solv:

$$S(m) = \sum_{k=-\infty}^{\infty} h(k).$$

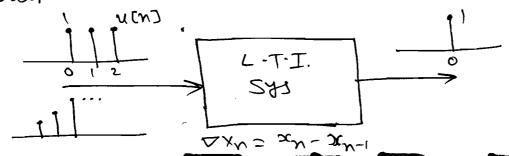
$$S(n) = \sum_{k=-\infty}^{\infty} (0.5)^k \cdot N(k).$$

$$= \sum_{k=0}^{\infty} (0.5)^k.$$

$$= 1 + (0.2) + (0.2)^{2} + (0.2)^{3} + \cdots + (0.8)^{n}.$$

$$S(n) = \frac{1 - (0.5)^{n+1}}{1 - 0.5}$$
; $n > 0$.

P2.3.2. An LTI System with Input u(n)
Produces the ordput of 8(n), then find the
Output due to the input hu(n)?



$$OP = mu(m) - (m-1) u(m-1).$$

$$= nu(m) - mu(m-1) + u(m-1).$$

$$= n (um) - u(m-1) + u(m-1).$$

$$= n s(m) + u(m-1).$$

$$= 0 + u(m-1).$$

$$OIP = u(m-1).$$

(E)

()

0

(_)

0

0

0

S(n) = u(n) - u(n-1)

P2.3.5.) Find the Overall impuse desponse for the interconnected system shown in bigure?

Zoin:

$$h(t) = \left[-\left[\left[h_2(t) + h_3(t) \right] * h_4(t) \right] + h_1(t) \right] * h_5(t).$$

Fourier Series:

- → It is an approximation Process where a non-simusoidal waveform is converted for simusoidal such that all the Periodic signal are represented as in unique form.
- Sinusoids and Complex exponents are eigen functions at LTI System.

 (Sume old as input)
- > For a signal to have tourier series, orthogonality is must condition. (Two signal X,(t) and X2(t) are orthogonal it \(\) \(
 - -> Means area under inner Product inner Product Of Iwo signer is zero.

Forguency	Continuous	Discoete
Continuous	C.T.F.T.	D. T. F.T.
Biscrete	C.F.S.	D.F.T.

Period -> many toez. one $\omega_{\circ} \longrightarrow \gamma \omega_{\circ}$. > These use 2 seasons for evaluating the F.S. 1. To obtain un expression bos that applies everywhere, rather Single period. ould ones a each harmonic of the waveform.

2. To obtain phasor, which indirectly ten how much power is available at

Trignometric Fourier Series

0, Wo, 260, 360, --

x(t) = 0,001(0.00) + 0,00100t + 02(0]20,t + 97 (0) 3 wot + 94 (0)4wot + ... + bo sin (o.w.t) + b, sin wet + be sin (200t) + b3 sin 300, t+ ...

 $x(t) = a_0 + \sum_{n=1}^{\infty} a_n cos n \omega_0 t + b n sin \omega_0 n t.$ C.C.

(F)

()

(:)

()

 (\cdot)

()

0

()

()

 $\left(\cdot \right)$

(')

$$\Rightarrow \int_{0}^{\infty} \cos \omega_{0} dt = \int_{0}^{\infty} \sin \omega_{0} nt dt = 0$$

$$n \neq 0$$

$$\Rightarrow \int_{0}^{\infty} \sin \omega_{0} nt dt = \int_{0}^{\infty} \sin nt dt = 0$$

$$\Rightarrow \int_{0}^{\infty} \cos \omega_{0} nt dt = \int_{0}^{\infty} \sin nt dt = 0$$

$$\Rightarrow \int_{0}^{\infty} \cos \omega_{0} nt dt = \int_{0}^{\infty} \sin nt dt = 0$$

$$\Rightarrow \int_{0}^{\infty} \cos \omega_{0} nt dt = \int_{0}^{\infty} \cos nt dt = 0$$

$$\Rightarrow \int_{0}^{\infty} \sin t e g c t dt q dt = \int_{0}^{\infty} a_{0} dt + \int_{0}^{\infty} a_{0} t dt = \int_{0}^{\infty} a_{0} dt + \int_{0}^{\infty} a_{0} t dt = \int_{0}^{\infty} a_{0} dt + \int_{0}^{\infty} a_{0} t dt = \int_{0}^{\infty} a_{0} dt + \int_{0}^{\infty} a_{0} dt = \int_{0}^{\infty} a_{0} dt = \int_{0}^{\infty} a_{0} dt + \int_{0}^{\infty} a_{0} dt = \int_{0}^{\infty} a_{0} dt = \int_{0}^{\infty} a_{0} dt = \int_{0}^{\infty} a_{0} dt + \int_{0}^{\infty} a_{0} dt = \int_{0}^{\infty}$$

=> Multiply both side ob ear - 1) by

(as wont & integrating both side of or

ear - 0) then we get,

Then we get,

Then coswont at a sincertate

the standard of the coswont incompation of the coswont. Sincertate

the standard of the coswont. Sincertate

the standard of the coswont.

 $\therefore \int g(t). \cos \omega_{ont} dt = \alpha_{n}. \left(\frac{1}{2}\right)$ $\therefore \int q_{n} = \frac{2}{T} \times \int g(t). \cos \omega_{ont} dt.$

* Polas form:

g(1)= 0, do + 5 dn (0) (wont + 8n).

(of) do + sin (wont + on).

()

 \bigcirc

fore convienent are will use cosine.

gapl= d0 + 5 dn c05 (wont + 8m).

1. g(x)= do + \sum_{n=1}^{\infty} dn (oswont. coson - dn sinwont. sinon. an= dn (0) On, bn=-dn. sinon. 00 = 90. | | dn | = Nan2 + pn2 = magnitude spectarm. Amplitude Speltrum. / dn/ Mote: Form the magnitude Speltourn we

will inform that for what range of foer. the max. Power is concentrated. * Effect of zhumeting an leasier forms

Symmety	Condition	Cro	Cen	bn.
Even	3(F)= 3(-F)	۶ _.	8.	0
0 4 4	8 (F) = -8(-F)	0	0	٤
Halb-	g(t) = -g(t= 7/2)	S	= 9; n-odd	= 8, N-099

a Find the TFS depresentation too the shown below. periodic wavetorm - T=2TT->1 $\omega_0 = \frac{2\pi}{T} = \frac{2\pi}{2\pi} = 1$ rud/sec. -> Her, odd- Symmetry. So, a, =0, 9x=0. $x(t) = \frac{1}{\pi}t$, $-\pi \leq t \leq \pi$. bn= = Tx(t). Sin wint. dt = 2 2TT (x(t). Sin a, ht. dt = 1 TT x(t). Sin won t dt = 2 x T T t. sin w.nt dt.

(=)

 \odot

(

(

()

$$= \frac{2V}{\Pi^2} \times \left[(t) \cdot \left(\frac{-\cos(\omega_0 nt)}{\omega_0 n} \right) - \cos(-\frac{\sin(\omega_0 nt)}{(\omega_0 n)^2} \right]_0^{\Pi_T}$$

$$\omega_0 = 1 \text{ study jet.}$$

$$= \frac{2V}{\Pi \Pi} \times \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \times \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \times \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \times \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \times \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \times \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi \Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

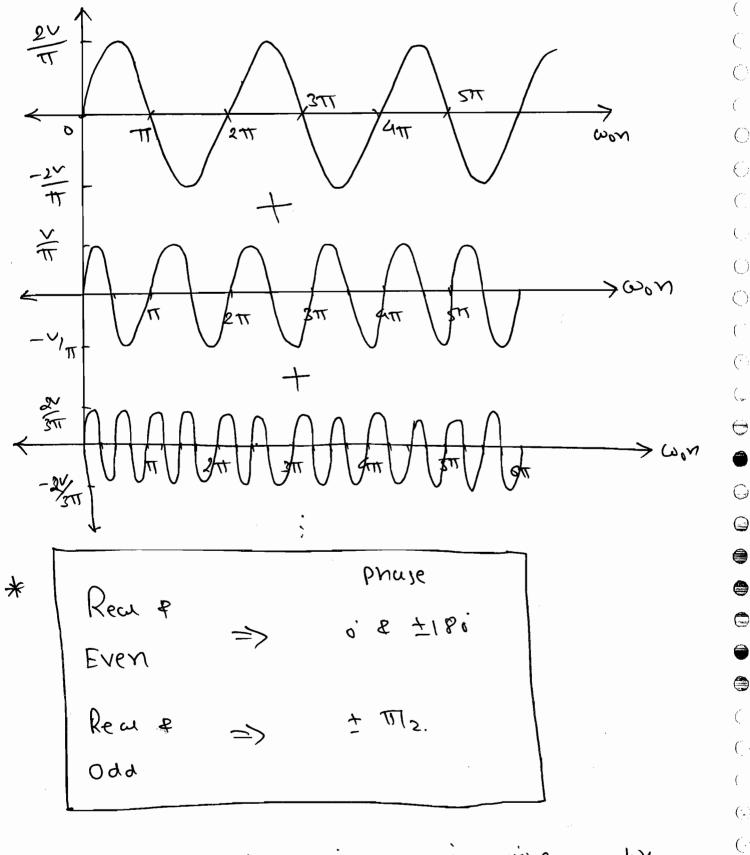
$$= \frac{2V}{\Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 \right)$$

$$= \frac{2V}{\Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 - 0 \right)$$

$$= \frac{2V}{\Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 - 0 \right)$$

$$= \frac{2V}{\Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 - 0 \right)$$

$$= \frac{2V}{\Pi} \cdot \left(\frac{-H}{n} \cdot \cos(n\pi) + 0 - 0 - 0 - 0 \right)$$



P3.2.1. A Periodic Signal is given by $x(t) = 3 \sin (4t + 30) - 4(0) (12t - 60) \text{ find}$ the amplitude of Second harmonics $x(t) = 3 \sin (4t + 30) - 4(0) (12t - 60).$ $x(t) = 3 \sin (4t + 30) - 4(0) (12t - 60).$

-> Wo= Cr-(.D. (4,12) = 4.

So, Amp. IInd har = 0. : Phase Of III sq harmonic = -60 ± 180. 1+10 => 0: -1+jo=) ± 180. +j => ± 90°. P.3.2.3 Find the T.F.J. sepresentation of the Periodic Signal xct) Shown in fig 3-2-39 It is a hidden Symmety,

Soin: It is a hidden symmetry, $\frac{1}{2} \times 2 \times 1 = 1.$ $\frac{1}{2} \times 2 \times 1 = 1.$

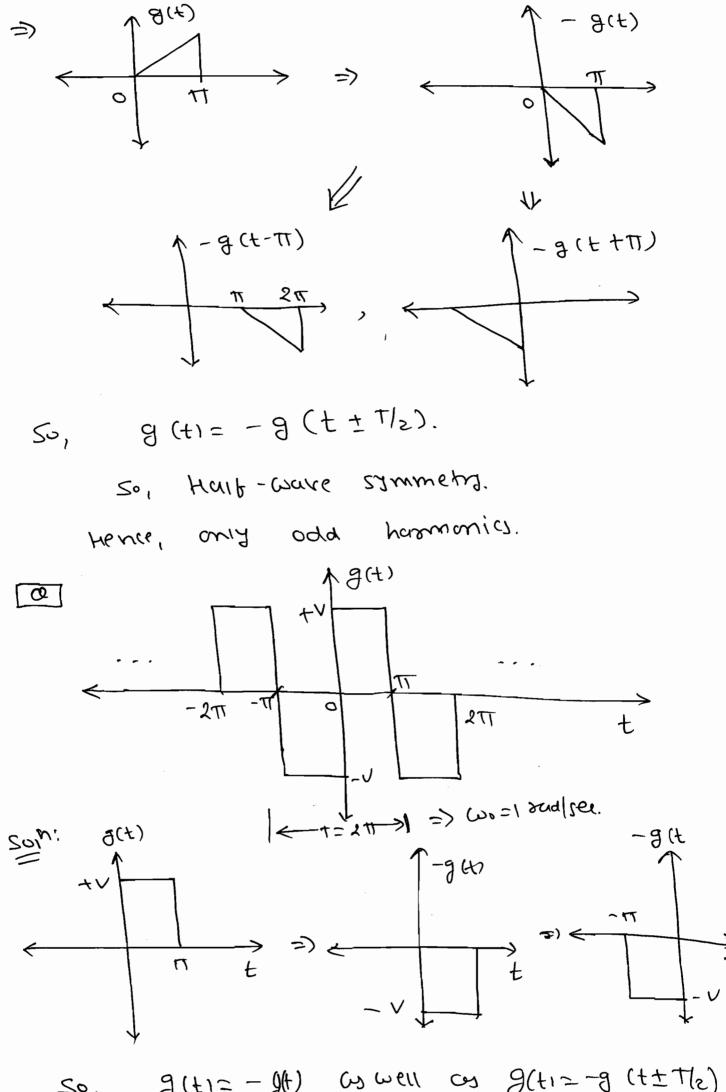
=) for hidden, symmetry we will get. Ou & by only.

Hidden odd: G. & bn. 6 Co=1 X(+1= 2+, 05+51. here, bn= 2 2t. sin won. dt Here, T=1 => W0=2TT $= \frac{2}{1} \times 2 \cdot \left[(t) \cdot \left(-\frac{(0) \omega_0 N}{(0) \omega_0 N} \right) - (1) \left(-\frac{\sin (\omega_0 N)^2}{(\omega_0 N)^2} \right) \right]$ $\frac{1}{2\pi n} \left[-\frac{1 \cdot (0)2\pi n}{2\pi n} + 0 - 0 - 0 \right]$ - 2 TM Show in @ [P3.2.4.] For the Periodic waveforms Eigure what what frez. Components are present in toignometric series expunsion. (P) K-712=7-=> Wo= 2TT = 1 Sad | Sel.

(P)

()

0



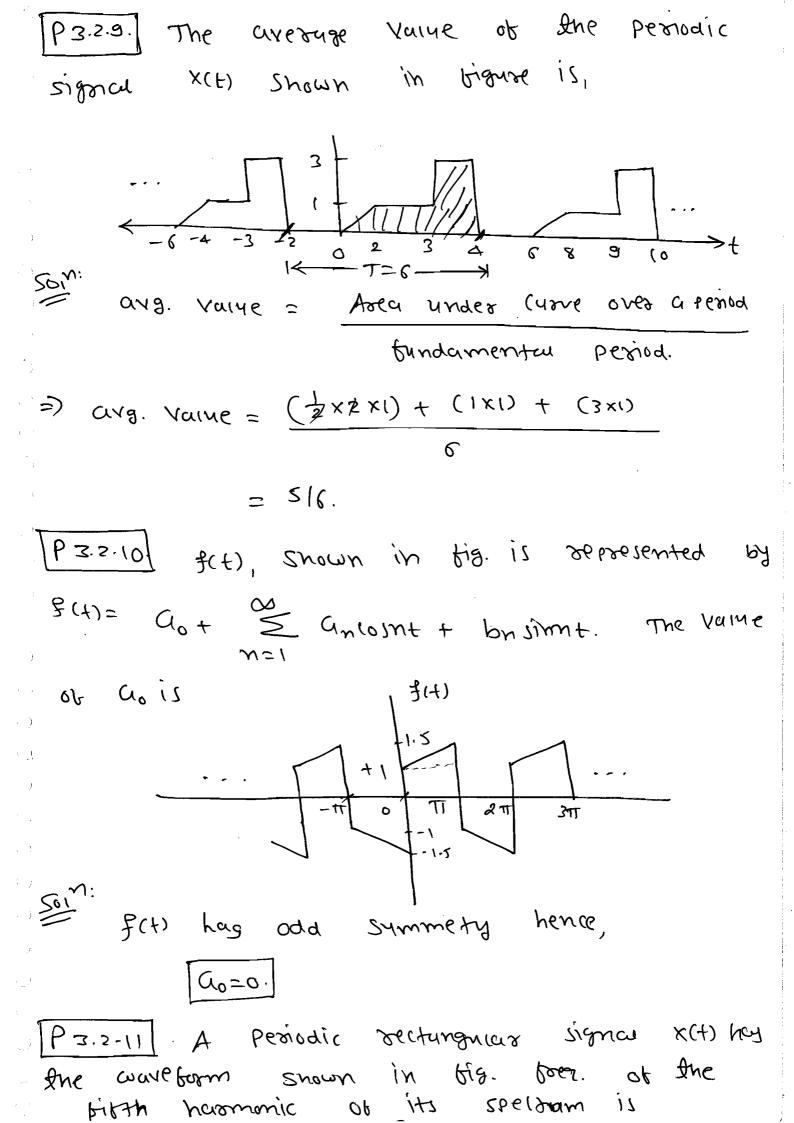
g(t1=- It) cos well as g(t1=-g (t±t/2).

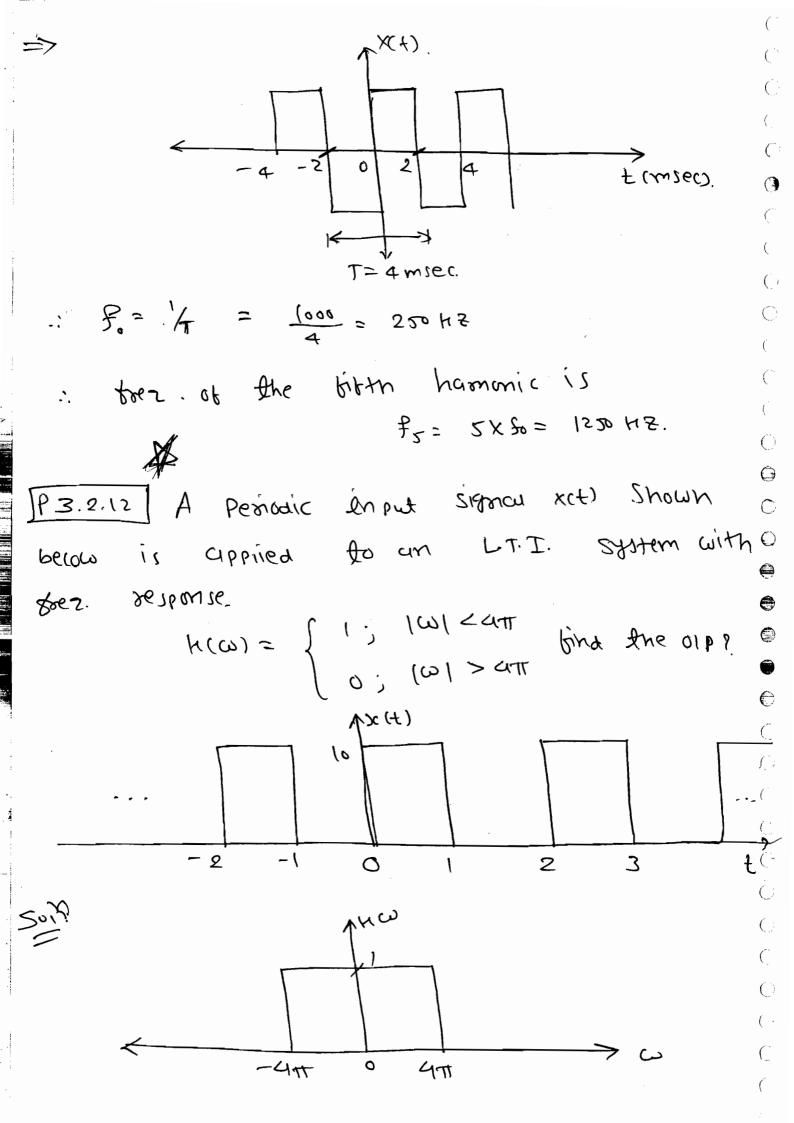
,-> Therefor given g(t) has odd and half. wave symmety both. Hence, sine terms with odd harmonics. 0 (R) \bigcirc () K-T=RT-X 2012 : Co= 1 malser. 0 and also So, It is a hart-wave Symmetry even symmetry. So, De De cosine terms with odd harming. Here, given mcf1 has even symmetry as () wen a hult-ware Symmetry. So, Cosine term, with odd harmonics

[P3.2.5.] Consider the signal x(t) = (0(0) (10TT+TTA) +4sin (30TH + M1). It's Power Wing within the becausing bund to Hz to 20 Hz is ____ Soli: $\omega_0 = (c.c.o.) (10TT, 30TT)$ So, Power in the feer bund long to 20 hz is 42 = 8W. (Q-3.2.6) Consider the toignometric series, which holds tome Ht, given by X(+) = sincot + = sinzwot + = sin swot + finzwot At Wo = I the sener (onverses to ___. 5017: at 00 = TT2 X(t)= 1- = + = - = + + ... = 71/4. tun'x= x- x2+ x3+-x4+x5+... メニノ タロップ(1)= 丁= 1- サナケー な+ な+…

is given by P3.2.7 A function f(t)= sin2t+ co12t. Which of the following is TRUES f(t) = Sin2t + Cos2t. => P(+1= 1- colst + colst. $= \frac{1}{2} + \frac{(012t)}{2}.$ 9=0 (= 2 => 5= /T. So, & how brequency Components at a and ()() /T HZ. \mathbf{C} [P3.2.8.] (a) The fundamental trea. Of the \cdot signal. 0 X(+1= 2+3(0)(0.2+) + co) (0.25++ TT2) (3) +.e.co1 (0.3+-17) is -. (00= CT-C-D. (0.2, 0.25, 0.3). = 0.05 (4,5,6).So, Wo= 0.05. And | see. (b) For a periodic signal V(t) = 30 sin lost t (0005 300t + 6 sin (500f + TT/4), Ine fundamentas frez. in suals is. Q. = CT. (.O. (100, 300, 500).

 $\omega_0 = 100$ rad 15.





$$\Rightarrow \omega e \quad \text{Should} \quad \text{find} \quad \text{fit} \quad \text{in} \quad \text{foet. domain}.$$

$$T = 2 \quad =) \quad \omega_0 = \frac{2\pi}{2} = TT$$

$$Q_0 = \frac{10\pi I}{2} = 5.$$

$$Q_{10} = \frac{2}{T} \quad \text{fit} \quad \text{(c)} \quad$$

$$X(t) = 5 + \frac{80}{20} \frac{10}{100} \left[1 - (-1)^{2}\right] \cdot SANCWN.$$

$$X(t) = 5 + \frac{20}{10} \cos(\omega n) + \frac{20}{317} \cos(\omega n)$$

$$+ \frac{20}{577} \cos(\omega n) + \cdots$$

$$X(t) = 5 + \frac{20}{10} \cos(\omega n) + \frac{20}{317} \cos(\omega n)$$

$$+ \frac{20}{577} \cos(\omega n) + \cdots$$

$$X(t) = 5 + \frac{20}{100} \cos(\omega n) + \frac{20}{317} \cos(\omega n)$$

$$X(t) = 5 + \frac{20}{100} \cos(\omega n) + \frac{20}{317} \cos(\omega n)$$

$$+ \frac{20}{577} \cos(\omega n) + \cdots$$

$$+ \frac{20}{577}$$

()

()

()

(

0

: g(t) = Co + \(\sigma \) Cn.e + \(\sigma \) (-n.e . Put n=-m = 5 (n.e :. g(t)= Co + ∑ cn.e + ∑ cn.e + ∑ cn.e $g(t) = \sum_{N=-\infty}^{\infty} C_{N} \cdot e$ => tre and - re begs. denotes opposite disection of solution i.e. Opposite phase omgre. => -00to +00 so, two sided -ve brea (-300 -200 -600) 0 Consider because Reproducing the sommer signed

T. F.s. to E. F.s.: 100 - 90 an- 1bn $c_n = \frac{1}{\tau} \int_{-\infty}^{\infty} g(t) \cdot e \cdot dt$ jount $C-n = \frac{a_n + ib_n}{2} = \frac{1}{\tau} \int g(t) \cdot e \cdot dt$ 0 E-F.S. to obtain the E.F.s. representation of P 3.2.15 signed shown, hence find the perio di (T-F.J. 8. x(+)

T= 1=) W=2TT

(:

Soin: X(t)= t, O< E<1.

WO = 277

Lan= II, many.

= - T, add,

$$C_{n} = \frac{1}{T} \int_{0}^{T} x(t) e . dt$$

:
$$C_{n} = \frac{1}{1} \int_{1}^{1} t \cdot e \cdot t \cdot$$

$$Cu = \left[(f) \left(\frac{-isuu}{6} \right) - (1) \left(\frac{(suu)_5}{6} \right) \right]^0$$

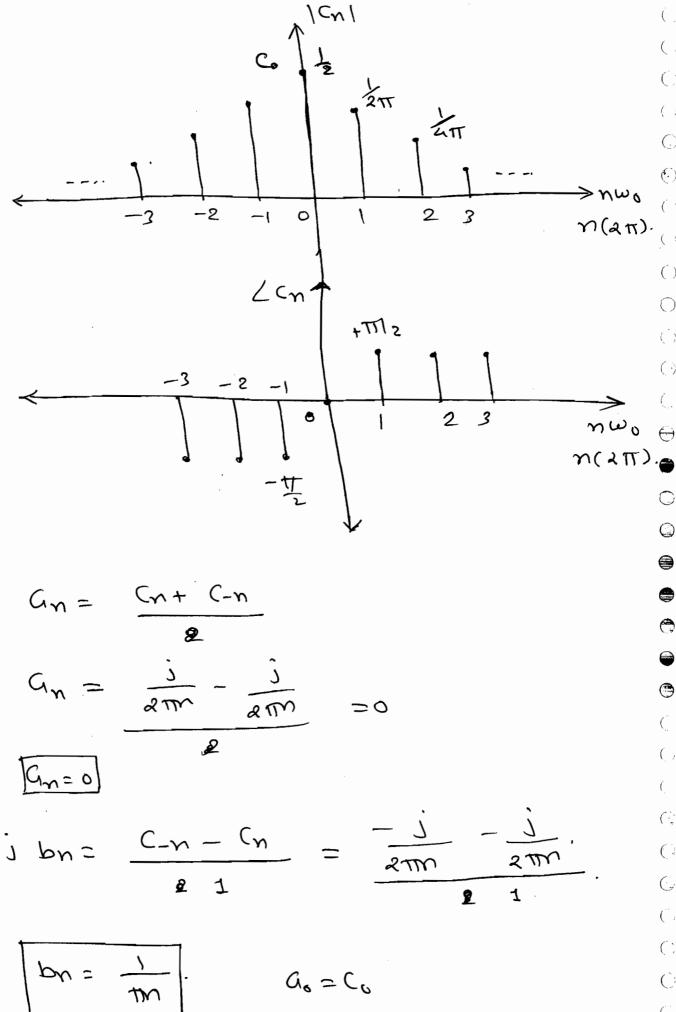
$$c_{n} = \frac{-i3\pi n}{-i3\pi n} - \frac{(3\pi n)^{2}}{2} + \frac{(3\pi n)^{2}}{6}$$

$$= \frac{j}{2\pi m^2} - \frac{1}{2\pi m^2} + \frac{1}{(2\pi m)^2}$$

$$C_{n} = \frac{j}{2\pi n}$$
, $C_{-n} = \frac{-j}{2\pi n}$

$$|C_n| = \left| \frac{1}{2\pi n} \right|$$

$$|C_n| = \frac{1}{2\pi n}, \quad |C_0| = \frac{1}{2}.$$



4.=/2

()

()

$$|dn| = \sqrt{0 + (\frac{1}{m})^2}$$

$$C_{5} = \frac{4}{2j}$$

$$C_{5} = \frac{4}{2j}$$

$$C_{5} = -2j$$

$$C_{6} = -2j$$

$$C_{7} = -2j$$

$$C_{7$$

 \bigcirc

 \bigcirc

()

()

 \bigcirc

0

(,

Note: Col Pu Carelbangs to du.

P3.2.16 Consider the two-sided signal signal Spectrum Shown in figure for x(t), find x(t)? Mug. 4 2 -28 - 75 12 F(He). -20 20 2 8 18.0 -12 -28 ري ہ ح f(he) -20

=> Polas from:

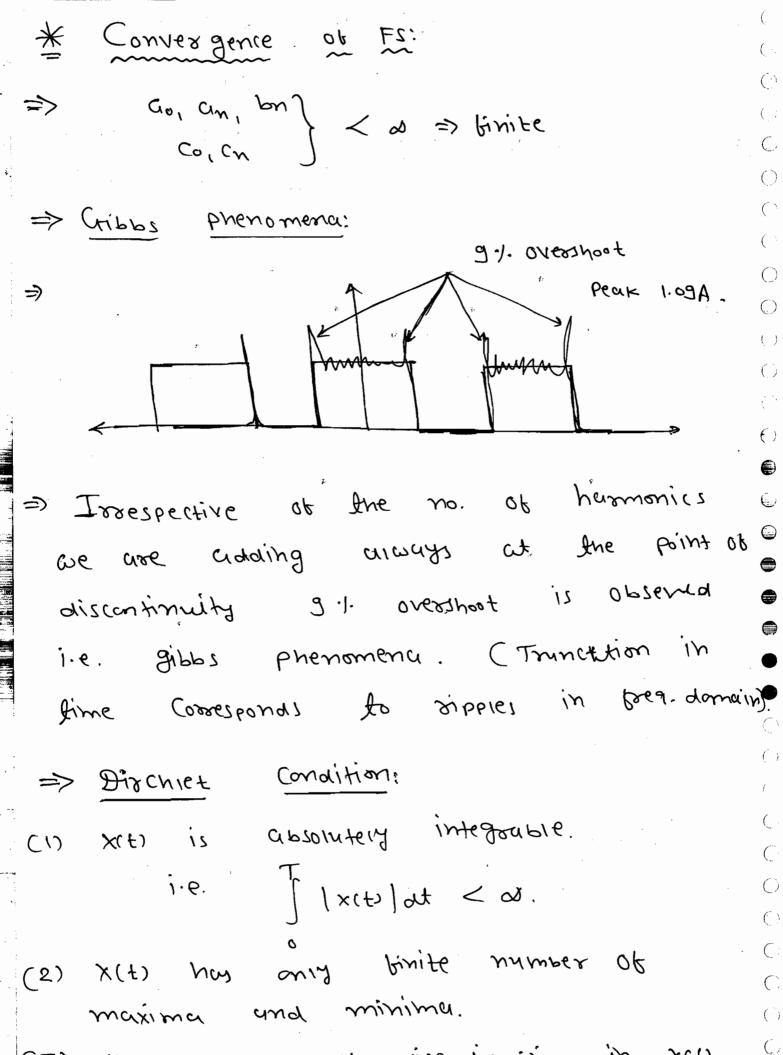
 $(\dot{})$

()

$$x(t)=d_0+\sum_{n=-\infty}^{+\infty}d_n cos(\omega_{0}nt+\omega_{n}).$$

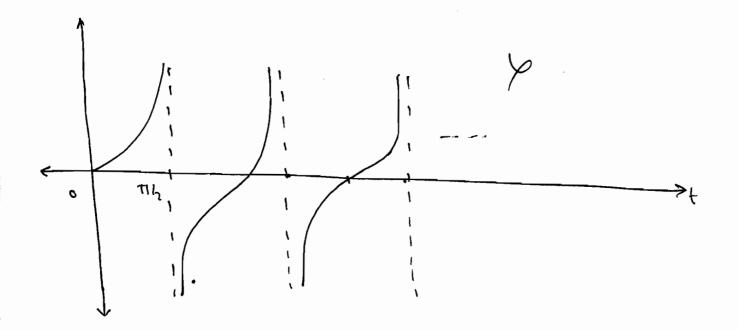
$$x(t) = 2 + 6(0) (2\pi (12)t + 180)$$

+ 8(0) (2\pi (20)t + 0').
+ 2(0) (2\pi (28) - 186).



(3) The sumber of discontinuities in x(1)

63.0 X(f)= f' O<f<1. Integrable. Gp201 Mer3 LON J(+) 2 2 3 - 2 finite discontinuity (3 to 4) Vaiid because 3 0 2 2 Valid because so many discontinuity. Not



Not vuid because within Ine limit it has infinite discontinuity.

 C_{i}

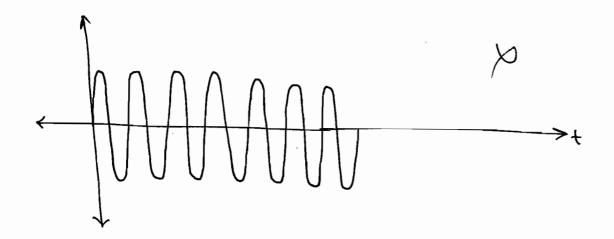
()

0

(j)

0

(5)
$$\chi(t) = Sin(\frac{2\pi}{t}), \quad 0 < t < 1.$$



=> Not valid more no. ob maxima & minima.

* Properties ob F.S:

(1) Lineasity:

 $\Rightarrow \text{Tf} \qquad \chi_{(t)} \longrightarrow C_{n}$ $\chi_{(t)} \longrightarrow d_{n}$

then $\alpha x_{i(t)} + \beta x_{i(t)} \longrightarrow \alpha (n + \beta d_{n})$

(2) Time Shift:

 $\Rightarrow IP \qquad x(f) \longrightarrow C^{\mu}$

 $4ne \quad \chi(t-t_0) \longrightarrow e^{-j\omega_0 n t_0}$

-> when we shift in the time-domain, it changes the phase of each harmonic in proportion to its free. nwo.

(3) Frequency Shitt:-

=) If $x(t) \longrightarrow C^{\nu}$

the $e \cdot x(t) \longrightarrow C_{n-m}$.

Mote: Shibting one domain Corresponds to Multiplication by exponential term in other domain.

[P3.3.1.] The F.s. Coefficient of signal X(t) Shown in fig(a) are Co = /11, C1=-10-25($C_n = \frac{1}{T(1-n^2)}$ (neven) Find F.S. coefficient 06 y(t), f(t) and g(t)? , X(F) 0 => Wo = 2TT = TT A(+) 3 5 => } (t = x(t-1). X(t) → Øn. -jwo(1). to X(t-1) = 7(t)

(

0

(

()

 \bigcirc

()

 \bigcirc

()

0

$$d_1 = C-13. C_1 = + 30.25$$

$$\therefore q^{\nu} = \frac{(1-\nu_s)}{(-\nu_s)} \quad (\nu \in N_s)$$

$$\Rightarrow$$
 4 f(t1= $x(t)$ - $x(t-1)$.

$$f(x) = x(t) - y(t).$$

Limeants

$$F_1 = -j_0.2$$

$$= -j_0.52 - j_0.52$$

(,,,

 $\left(\tilde{x}_{i,j}^{(k)}\right)$

 (\cdot)

()

 \bigcirc

 $(\Box$

(

0

 $(\overline{\ })$

0

()

 \bigcirc

()

 \bigcirc

$$g(f) = \chi(f) + \chi(f-1) = \chi(f) + \chi(f)$$

$$\frac{g_{N}=\frac{2}{2}}{\sqrt{2}} \cdot \frac{g_{N}}{\sqrt{2}} \cdot \frac{g_{N}}{\sqrt{2}$$

[P 3.3.2] Let X(t) be a periodic signal with period T and F.S. coethicient Cn. Let, Y(t)= x(t-to) + x(t+to). The F.S. Coefficient of 2(+) If dn=0 & odd n fnen to can be a) T18 b) T14 c) T12 d) 2T. A(f) = X(f-fo) + x(f+fo). $-j\omega_{0}nt_{0}$ $dn = e \cdot c_{n} + e \cdot c_{n}.$ $dn = 2 cn \left[\frac{j \omega_{\text{onto}}}{e} + \frac{-j \omega_{\text{onto}}}{e} \right].$: dn = 2 Cn Cos wonto. => dn=0 when la workto = nodd. : Wo. to = TT. : 2th to= 1/2 : [to= T/4] ~ 4) Time - Scaling: => X(t) -> Cn/T, wo

X(Xt) --> Cn/T/x, dwo.

Time - Compressing by a changes beginning from Go to dwo.

$$\rightarrow \chi(t) = \sum_{n=-\infty}^{+\infty} C_{n} \cdot e$$

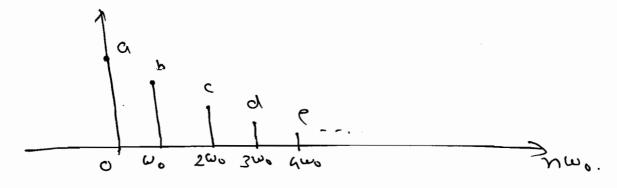
$$\therefore \chi(dt) = \sum_{n=-\infty}^{+\infty} c_n \cdot e \cdot .$$

MOW,
$$W_0' = \chi W_0$$
.

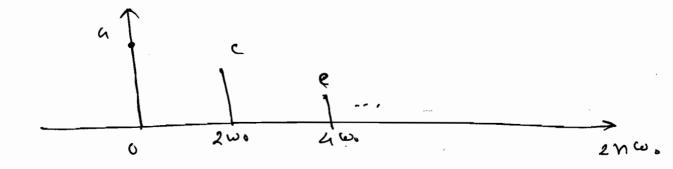
$$\frac{2\pi}{\tau'} = \chi \times 2\pi$$

$$\frac{7}{\tau} = \frac{1}{2} \times \frac$$

e.g.
$$\chi(t) \longrightarrow C_{\gamma}/\omega_{0}$$



$$\Rightarrow$$
 $\chi(2t) \rightarrow cn/2\omega_0$



C

 \bigcirc

0

()

 \bigcirc

O C

0

C

(. (.)

 \bigcirc

 \bigcirc

 \circ

 \bigcirc

Mote: Compression in time domain is expunsion in bear domain. (5) Dibberentiation in Jime: => X(t) <--> Cn. $\frac{dx(t)}{dx(t)} \longleftrightarrow (j\omega_{oN}) C_{n}$: dk x(t) (jwin) Cn. P3.3.3) By using desirative method, find F.s. Coefficient of the signal shown in figure ? ×(+) 915 라 x(+)

$$y(t) = \frac{d}{dt} \times (t).$$

$$\frac{T}{T} = \frac{1}{T} \int y(t) \cdot e \cdot \omega t \cdot \frac{1}{T} \int y(t) \cdot e \cdot \omega t \cdot \frac{1}{T} \int y(t) \cdot e \cdot \omega t \cdot \frac{1}{T} \int y(t) \cdot e \cdot \omega t \cdot \frac{1}{T} \int y(t) \cdot e \cdot \omega t \cdot \frac{1}{T} \int y(t) \cdot e \cdot \omega t \cdot \frac{1}{T} \int y(t) \cdot e \cdot \omega t \cdot \frac{1}{T} \int y(t) \cdot e \cdot \omega t \cdot \frac{1}{T} \int y(t) \cdot e \cdot \omega t \cdot \frac{1}{T} \int y(t) \cdot e \cdot \omega t \cdot \frac{1}{T} \int y(t) \cdot e \cdot$$

$$\therefore dn = \frac{1}{T} \int_{0}^{T} \left[8(t+d_{12}) - 8(t-d_{12}) \right]$$

$$= \frac{1}{T} \int_{0}^{T} \left[8(t+d_{12}) - 8(t-d_{12}) \right]$$

$$= \frac{1}{T} \int_{0}^{T} \left[8(t+d_{12}) - 8(t-d_{12}) \right]$$

$$= \frac{1}{T} \int_{0}^{T} \left[8(t+d_{12}) - 8(t-d_{12}) \right]$$

Mow,
$$\int_{0}^{t_{2}} 8(t-t_{0}) \cdot \chi(t) dt = \chi(t_{0}) \cdot$$

$$= t_{1} \leq t_{0} \leq t_{2}.$$

:.
$$qu = \frac{1}{2} \left[6 - 6 - 100 \cdot 100 \cdot 100 \right]$$

$$dn = \frac{2j}{T} \left[\begin{array}{c} j\omega \circ n d \\ e \\ - e \end{array} \right]$$

$$\therefore dn = \frac{2j}{T} \times \sin \omega_{on} d$$

$$= \frac{2}{7 \times \frac{2\pi t}{T}} \times \frac{1}{5} \times$$

$$d_{N} = (1\omega_{N})^{2}. C_{N}.$$

$$C_{N} = \frac{d_{N}}{d_{N}}.$$

$$C_{N} = \frac{d_{N}$$

 $q^{N=}-N = \left|\begin{array}{c} m^{0}l=3m^{0} \\ -|\mu| \end{array}\right|$

(b)
$$y(t) = \frac{d}{dt} x(t)$$
.

 $d_{N} = (j\omega_{0}n) \cdot (n \cdot | \omega_{0} = tT)$
 $d_{N} = (j\pi n) \cdot (-n) \cdot e^{-(n)}$.

 $d_{N} = -j\pi n^{2} \cdot e^{-(n)}$.

 $d_{N} = -j\pi n^{2} \cdot e^{-(n)}$.

 $d_{N} = e^{-j\omega_{0}n(1)}$.

 $d_{N} = e^{-j\omega_{0}n(1)$

()

 $\chi^{I}(f) = \frac{5}{\chi(f) - \chi_{*}(f)}$

$$\frac{(x_{1})}{2} = \frac{x_{1}(1+x^{*}(1)+x^$$

Soin:
$$y(t) = \left[\frac{j u \pi t}{2} - j u \pi t \right] \times (t).$$

$$E m = 4$$

$$j u \pi t - j u \pi t$$

$$y(t) = e \cdot x(t) + e - x(t).$$

$$dn = \frac{C_{n-4} + C_{n+4}}{2}$$

$$dn = -(n-4) \cdot 2 + -(n+4) \cdot 2$$

=> The fold average Power in Periodic signal is earch to the Sum of the Squared amplitude of each harmonics.

$$\chi(t) \Leftrightarrow C_n \text{ even} \left[\frac{1}{\tau} \int_0^{\tau} |\chi(t)|^2 dt = \int_0^{+\infty} |C_n|^2 \right]$$

•

() ()

0

 \bigcirc

C

[P3.3.6.] Find the Power up to II harmonic periodic signal shown in lighter too the X(F) from a: 3.2.12 =) Amp: 10 bn = 30 (odd n). Amp= 1 So, Co = Co = 1/2. $Cn = \frac{4n - jbn}{2} = -\frac{j}{2} \left(\frac{2}{n\pi}\right) = -\frac{J}{n\pi} \pmod{n}.$ => Power required upto II harmonic. P = \frac{12}{5} | Cn12. P= 1 C-212+ 1 C-1 2 + 1 C012+ 1 C1 2+1 C212 $= \frac{1}{(2\pi)^2} + \frac{1}{(11)^2} + \left(\frac{1}{2}\right)^2 + \frac{1}{(11)^2} + \left(\frac{1}{2\pi}\right)^2.$ P = 0.45 WUHS.

carculation of total power:
$$P = \frac{1}{T} \int_{0}^{T} 1 \times (4)^{2} dt$$

$$= \frac{1}{T} \int_{0}^{T} (1)^{2} dt.$$

P= 0.5 WUHH

Maximum Energy (as) bomer of any Note: signal is crownys these only in the low bez. region.

[P3.3.7] The F.S. Coefficients, Ob a periodic Signal X(t) is expressed on X(t) = E Che ihout use given by $C^{-5} = 5 - 11$; $C^{-1} = 0.2 + 10.5$; $C^{0} = 15$;

c1=0.2-10.5; c5= 5+11; cN=0 pax m1>2.

()

0

 \bigcirc

 \bigcirc

 \bigcirc

0

()

0

 \bigcirc

()

 \bigcirc

()

(

 (\cdot)

(-

.(

(:

⟨`.

Which of the following is TRUE ? (a) X(t) has finite energy because only knitery many (officients are non zero. (P) X(f) por sero areande raine pecanse it is periodic.

(c) the imaginary part of x(t) it is constant. (d) the seal part of X(t) is even.

Soin: -> Every periodic signal is power

Signal. and it energy is ∞ .

So option A is arong.

-> As (0 = 12 is given i.e *xct)

has non zero cherage vame and it

it indicates it is complex. hence

Option b is also wrong.

 $x(f) = x^{k}(f) + x^{k}(f)$

 $\therefore C_{n=} + \int_{-\infty}^{+\infty} \chi(t). \quad e^{-j\omega_0 nt} dt.$

 $= \frac{1}{T} \int_{-\infty}^{\infty} \left[x_{R}(t) + x_{\underline{1}}(t) \right] \cdot e \, dt.$

 $C_0 = 0 + j2 (constant)$

So, real part of xct) is o.

hence, the imaginary part of x(t) is constant.

So, Ans -> C.

* System with Periodic Inputs: $\text{SIP } x(f) = 6 \xrightarrow{\text{Post}} \text{OIB } A(f) = 6 \cdot P(m).$ \rightarrow $\beta(t) = \int \chi(t-\tau). \ \mu(\tau) \ d\tau.$ $= \int_{0}^{+\infty} e^{j\omega(t-\tau)} \cdot h(\tau) d\tau.$ = e . t ~ -jw7 = e . h(7).d7. y(t) = ejωt, μ(ω), y(t) = € Cn. H(nwo). e jnou ot P3.4.1 Find the output Voltage of the System Shown in figure, it the input Voltage is actio 4 coset Ralas \propto (4)

0

C

() ()

 \bigcirc

(

0

()

 \bigcirc

O Ċ

 (\cdot)

Ç

$$\frac{dy(t)}{dt} + y(t) = x(t).$$

$$H(\omega) = \frac{1}{1+i\omega},$$

:
$$H(n\omega_0) = \frac{1}{1+j\omega_0 n} = \frac{1}{1+j2n}$$

=)
$$x(t) = (x\cos 2t) + j(x\cos 2t) + 2e$$

:
$$y(t) = 2\left[\frac{1}{1+i2}\right]e^{i2t} + 2\left[\frac{1}{1-i2}\right]e^{-i2t}$$

() () ()() () () \bigcirc () () (∙) ()(_) \bigcirc ()(', () \bigcirc (_) ()()